

**NOTE:**

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**NOTA:**

- As 'n kandidaat 'n vraag TWEEKEER beantwoord, merk slegs die EERSTE poging.
- As 'n kandidaat 'n poging om die vraag te beantwoord, doodgetrek het en nie dit oorgedoen het nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienmemorandum toegepas.
- Aanvaarding van antwoorde/waardes om 'n probleem op te los, is ONaanvaarbaar.

**VRAAG/QUESTION 1**

1.1	$a = 16,16$ (16,1571639) $b = 0,88$ (0,8847043972) $\hat{y} = 16,16 + 0,88x$	answ only:full marks	✓ $a$ ✓ $b$ ✓ equation	(3)
1.2	$\hat{y} = 16,157\dots + 0,884\dots$ (73) = 81%	answ only:full marks	✓ Subst into eq ✓ Answer (accept 80%)	(2)
1.3	$r = 0,92$ (0,9177373213)		✓ ✓ Answer (accept 0,91)	(2)
1.4	Yes./Ja The correlation between the two exams is very strong/ Die korrelasie tussen die twee eksamens is baie sterk..		✓ Yes ✓ correct justification	(2)
				[9]

**QUESTION/ VRAAG 2**

2.1	Modal Class: $19 \leq t < 23$	✓ ✓ answer	(1)	
2.2	<p style="text-align: center;"><b>OGIVE - OGIEF</b></p>	<ul style="list-style-type: none"> <li>✓ grounding at (11;0)</li> <li>✓ plotting upper limits</li> <li>✓ plotting cumulative frequency</li> <li>✓ drawing a smooth curve</li> </ul> <ul style="list-style-type: none"> <li>✓ geanker by (11;0)</li> <li>✓ plot boonste limiete</li> <li>✓ plot kumulatiewe frekwensie</li> <li>✓ gladde kurwe</li> </ul>	(4)	
2.3	$Q_1 = 17,5$ (accept 17 – 18 ) $Q_3 = 25,5$ (accept 25 – 26) $IQR/IKO = 25,5 - 17,5$ $= 8$ (accept 7 – 9)	<ul style="list-style-type: none"> <li>✓ 17,5</li> <li>✓ 25,5</li> </ul> <ul style="list-style-type: none"> <li>✓ answer</li> </ul>	(3)	
2.4	Read off from graph: 18 occasions $\therefore 48 - 18 = 30$ times	<div style="border: 1px solid black; padding: 2px; display: inline-block;">answ only:full marks</div>	<ul style="list-style-type: none"> <li>✓ accept 17 – 18</li> <li>✓ answer</li> </ul>	(2)
			[10]	

**QUESTION/ VRAAG 3**

3.1	$m_{BC} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{BC} = \frac{0 + 8}{-5 - 1}$ $m_{BC} = \frac{8}{-6} = -\frac{4}{3}$	✓ Substitution ✓ Answer	(2)
3.2	$E = \left( \frac{x_2 + x_1}{2}; \frac{y_2 + y_1}{2} \right)$ $= \left( \frac{-5 + 1}{2}; \frac{0 - 8}{2} \right)$ $= (-2; -4)$	✓ $x$ value ✓ $y$ value	(2)
3.3	$m_{DE} = \frac{3}{4}$ [DE $\perp$ BC] $y - (-4) = \frac{3}{4}(x - (-2))$ OR $-4 = \frac{3}{4}(-2) + c$ $y = \frac{3}{4}x - 2\frac{1}{2}$	✓ $m_{DE}$ ✓ Substitute $m_{DE}$ and E(-2 ; -4) ✓ equation	(3)
3.4	$\tan \theta = m_{AD}$ $\tan \theta = -\frac{4}{3}$ $\theta = 180^\circ - 53,13^\circ$ $= 126,87^\circ$	✓ $\tan \theta = -\frac{4}{3}$ ✓ $53,13^\circ$ ✓ answer (obtuse)	(3)
3.5	$\hat{\text{OFD}} = 126,87^\circ - 90^\circ$ [ext $\angle$ of $\Delta$ ] $= 36,87^\circ$	✓ method ✓ answer	(2)
3.6	$(5\sqrt{2})^2 = (-5 - x)^2 + (0 - 7)^2$ $50 = (-5 - x)^2 + (0 - 7)^2$ $50 = x^2 + 10x + 25 + 49$ $x^2 + 10x + 24 = 0$ $(x + 6)(x + 4) = 0$ $x \neq -6$ or $x = -4$	✓ Subst into dist formula ✓ $AB^2 = 50$ ✓ standard form ✓ factors ✓ correct choice	(5)
3.7	$(x - a)^2 + (y - b)^2 = r^2$ $(x - (-2))^2 + (y - (-4))^2 = (-5 - (-2))^2 + (0 - (-4))^2$ $(x + 2)^2 + (y + 4)^2 = (-5 + 2)^2 + (0 + 4)^2$ $(x + 2)^2 + (y + 4)^2 = 25$ OR $(x + 2)^2 + (y + 4)^2 = r^2$ $(-5 + 2)^2 + (0 + 4)^2 = r^2$ $(x + 2)^2 + (y + 4)^2 = 25$ OR $(x + 2)^2 + (y + 4)^2 = r^2$ $(1 + 2)^2 + (-8 + 4)^2 = r^2$ $(x + 2)^2 + (y + 4)^2 = 25$	✓ Subst LHS ✓ Subst RHS ✓ Answer ✓ Subst LHS ✓ Subst (-5 ; 0) ✓ Answer ✓ Subst LHS ✓ Subst (1 ; -8) ✓ Answer	(3)
			[20]

**QUESTION/ VRAAG 4**

4.1.1	$x^2 + y^2 + 4x - 4y - 12 = 0$ $(x+2)^2 + (y-2)^2 = 12 + 4 + 4 = 20$ $M(-2 ; 2)$ OR $M\left(\frac{4}{-2}; \frac{-4}{-2}\right)$ $M(-2 ; 2)$	✓ $x$ value ✓ $y$ value  ✓ $x$ value ✓ $y$ value	(2)
4.1.2	$x^2 + 0^2 + 4x - 4(0) - 12 = 0$ $x^2 + 4x - 12 = 0$ $(x+6)(x-2) = 0$ $x \neq -6$ and $x = 2$ , $C(2 ; 0)$ OR $\frac{x_C - 6}{2} = -2$ $x_C = 2$ $C(2 ; 0)$	✓ $y$ - coordinate = 0 ✓ factors ✓ correct $x$ value  ✓ correct use of formula  ✓ $x$ value ✓ $y = 0$	(3)
4.2	$m_{MC} = -\frac{1}{2}$ $m_{tangent} = 2$ [tangent $\perp$ diameter] $y - y_1 = m(x - x_1)$ $y - 4 = 2(x - (-6))$ $y = 2x + 16$	✓ S ✓ R ✓ substituting A(-6 ; 4) ✓ equation	(4)
4.3	B( $x ; 0$ ) $y = 2x + 16$ $\therefore 0 = 2x + 16$ $\therefore x = -8$ Area $\Delta ABC = \frac{1}{2} BC \times h$ $= \frac{1}{2}(10) \times 4$ $= 20$ sq units OR B( $x ; 0$ ) $y = 2x + 16$ $\therefore 0 = 2x + 16$ $\therefore x = -8$ $AB = \sqrt{(-6 + 8)^2 + (4 - 0)^2}$ $AB = \sqrt{20}$  <i>Area of <math>\Delta = \frac{1}{2}(AB)(AC)</math></i> $= \frac{1}{2}(\sqrt{20})(2\sqrt{20})$ $= 20$ unit <sup>2</sup>	✓ $y = 0$ in equation ✓ $x_B$  ✓ BC = 10 ✓ $h = 4$  ✓ answer  ✓ $y = 0$ in equation ✓ $x_B$  ✓ $AB = \sqrt{20}$  ✓ AC = 2 radius = $2\sqrt{20}$ ✓ answer	(5)

4.4	Eq of tangent parallel to AB through C: $y - y_1 = m(x - x_1)$ $y - 0 = 2(x - 2)$ $y = 2x - 4$  $\therefore -4 < k < 16$ OR $x^2 + (2x+k)^2 + 4x - 4(2x+k) - 12 = 0$ $5x^2 + 4xk - 4x + k^2 - 4k - 12 = 0$ $5x^2 + (4k-4)x + (k^2 - 4k - 12) = 0$ $\therefore \Delta > 0$ $(4k-4)^2 - 4(5)(k^2 - 4k - 12) > 0$ $-4k^2 + 64k + 256 > 0$ $k^2 - 16k - 64 > 0$ $(k-16)(k+4) > 0$ $\therefore -4 < k < 16$	<ul style="list-style-type: none"> <li>✓ subst C(2 ; 0) into equation</li> <li>✓ eq of tangent through C</li> <li>✓ -4</li> <li>✓ 16</li> <li>✓ between</li> </ul>	
			(5) [19]

**QUESTION/ VRAAG 5**

5.1.1	$\sin 149^\circ = \sin 31^\circ$ $= p$	✓ reduction ✓ answer	(2)
5.1.2	$\cos(-59^\circ) = \cos 59^\circ$ $= \sin 31^\circ$ $= p$	✓ co-ratio ✓ answer	(2)
5.1.3	$\cos 62^\circ = 1 - 2 \sin^2 31^\circ$ $= 1 - 2p^2$	✓ double formula  ✓ answer in terms of $p$	(2)
5.2	$(-\tan \theta)(\cos \theta)^2 + (-\cos \theta)(\sin \theta)$ $\left(-\frac{\sin \theta}{\cos \theta}\right)(\cos \theta)^2 - (\cos \theta)(\sin \theta)$ $-(\cos \theta)(\sin \theta) - (\cos \theta)(\sin \theta)$ $-2(\cos \theta)(\sin \theta)$ $-\sin 2\theta$	✓ $-\tan \theta$ ✓ $\cos \theta$ ✓ $-\cos \theta$ ✓ identity  ✓ simplify and add ✓ answer	(6)
5.3.1	$LHS = \frac{\sin 2x + \sin x}{\cos 2x + \cos x + 1}$ $= \frac{2 \sin x \cdot \cos x + \sin x}{2 \cos^2 x - 1 + \cos x + 1}$ $= \frac{\sin x (2 \cos x + 1)}{2 \cos^2 x + \cos x}$ $= \frac{\sin x (2 \cos x + 1)}{\cos x (2 \cos x + 1)}$ $= \frac{\sin x}{\cos x} = \tan x$ $= RHS$	✓ expansion of $\sin 2x$ ✓ correct expansion of $\cos 2x$  ✓ simplify numerator ✓ factorize numerator & denominator  ✓ Identity	(5)
5.3.2	$\cos x (2 \cos x + 1) = 0$ or $\tan x = \frac{1}{0}$ $x = 240^\circ$ or $270^\circ$	✓ $240^\circ$ ✓ $270^\circ$	(2)
			[19]

## QUESTION/ VRAAG 6

6.1	$\begin{aligned} \sin(x+30^\circ) &= \cos 3x \\ &= \sin(90^\circ - 3x) \\ x + 30^\circ &= 90^\circ - 3x + k \cdot 360^\circ \\ 4x &= 60^\circ + k \cdot 360^\circ \\ x &= 15^\circ + k \cdot 90^\circ \end{aligned}$ <p>or</p> $\begin{aligned} x + 30^\circ &= 180^\circ - (90^\circ - 3x) + k \cdot 360^\circ \\ -2x &= 60^\circ + k \cdot 360^\circ \\ x &= -30^\circ - k \cdot 180^\circ ; k \in \mathbb{Z} \end{aligned}$ <p>OR</p> $\begin{aligned} \sin(x+30^\circ) &= \cos 3x \\ \cos[90^\circ - (x+30^\circ)] &= \cos 3x \\ 90^\circ - (x+30^\circ) &= 3x + k \cdot 360^\circ \\ -4x &= -60^\circ + k \cdot 360^\circ \\ x &= 15^\circ - k \cdot 90^\circ \end{aligned}$ <p>or</p> $\begin{aligned} 90^\circ - (x+30^\circ) &= 360^\circ - 3x + k \cdot 360^\circ \\ 2x &= 300^\circ + k \cdot 360^\circ \\ x &= 150^\circ + k \cdot 180^\circ ; k \in \mathbb{Z} \end{aligned}$	<ul style="list-style-type: none"> <li>✓ co-ratio</li> <li>✓ equation</li> <li>✓ general solution</li> <li>✓ equation</li> <li>✓ general solution ✓ <math>k \in \mathbb{Z}</math></li> <li>✓ co-ratio</li> <li>✓ equation</li> <li>✓ general solution</li> <li>✓ equation</li> <li>✓ general solution ✓ <math>k \in \mathbb{Z}</math></li> </ul>	(6)
6.2.1		<ul style="list-style-type: none"> <li>✓ max tp's</li> <li>✓ min tp</li> <li>✓ x intercepts</li> </ul>	(3)
6.2.2	Period = $120^\circ$	✓ answer	(1)
6.2.3	$x \in [15^\circ ; 105^\circ]$ OR $15^\circ \leq x \leq 105^\circ$	<ul style="list-style-type: none"> <li>✓ <math>15^\circ</math></li> <li>✓ <math>105^\circ</math></li> <li>✓ notation (penalize by one if -30 or -150 is included)</li> </ul>	(3)
			[13]

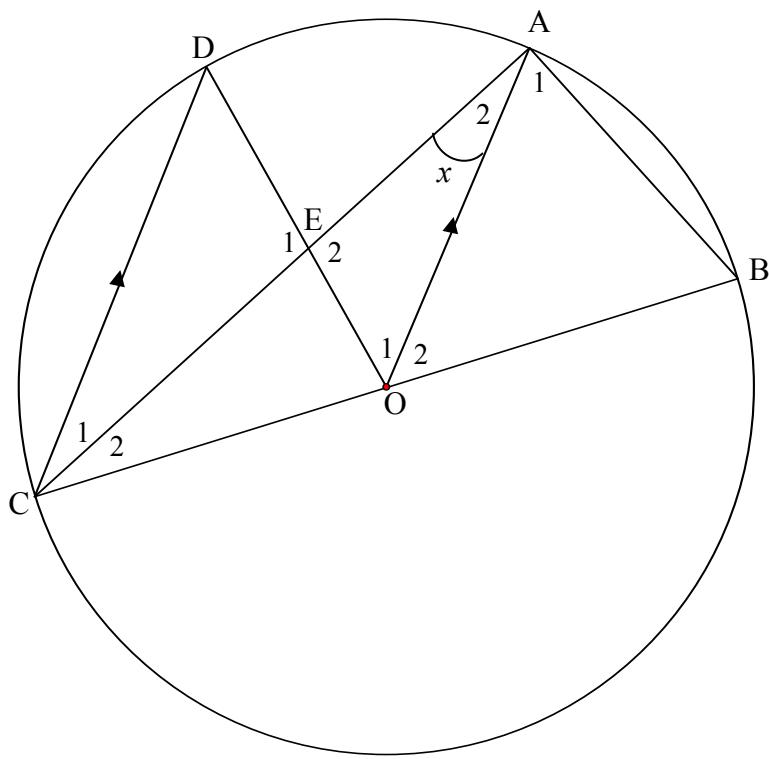
**QUESTION 7**

7.1	$\tan \alpha = \frac{AP}{AB}$ $AP = AB \tan \alpha$	✓ correct ratio ✓ AP into AB and $\alpha$	(2)
7.2	$\frac{AB}{\sin \beta} = \frac{20}{\sin(180^\circ - (\theta + \beta))}$ $\frac{AB}{\sin \beta} = \frac{20}{\sin(\theta + \beta)}$ $\therefore AB = \frac{20 \sin \beta}{\sin(\theta + \beta)}$ $\therefore AP = \frac{20 \cdot \sin \beta \cdot \tan \alpha}{\sin(\theta + \beta)}$	✓ correct subst into sine rule ✓ reduction ✓ AB as subject and subst into 7.1	(3)
7.3	$\theta = \beta$ [∠s opp equal sides] $AP = \frac{20 \cdot \sin \beta \cdot \tan \alpha}{\sin 2\beta}$ $AP = \frac{20 \cdot \sin \beta \cdot \tan \alpha}{2 \sin \beta \cdot \cos \beta}$ $AP = \frac{10 \cdot \tan \alpha}{\cos \beta}$	✓ replace $\theta$ ✓ expansion of $\sin 2\beta$ ✓ simplified answer	(3)
			[8]

**QUESTION/ VRAAG 8**

8.1	Line from centre to midpt of chord OR Line from centre bisects chord	✓ reason	(1)
8.2	$\hat{B} = 43^\circ$ [∠s in same segment]	✓ S ✓ R	(2)
8.3	$\hat{BAD} = 90^\circ$ [∠ in semi-circle] $= \hat{E}_1$	✓ S ✓ R	(2)
8.4	$BD = 28$ units $\therefore \cos 43^\circ = \frac{AB}{28}$ $\therefore AB = 28 \cos 43^\circ = 20,48$ units  OR $\frac{AB}{\sin 47^\circ} = \frac{28}{\sin 90^\circ}$ $\therefore AB = \frac{28 \sin 47^\circ}{\sin 90^\circ} = 20,48$ units	✓ correct ratio ✓ answer  ✓ correct ratio ✓ answer	(2)
			[7]

## QUESTION/ VRAAG 9

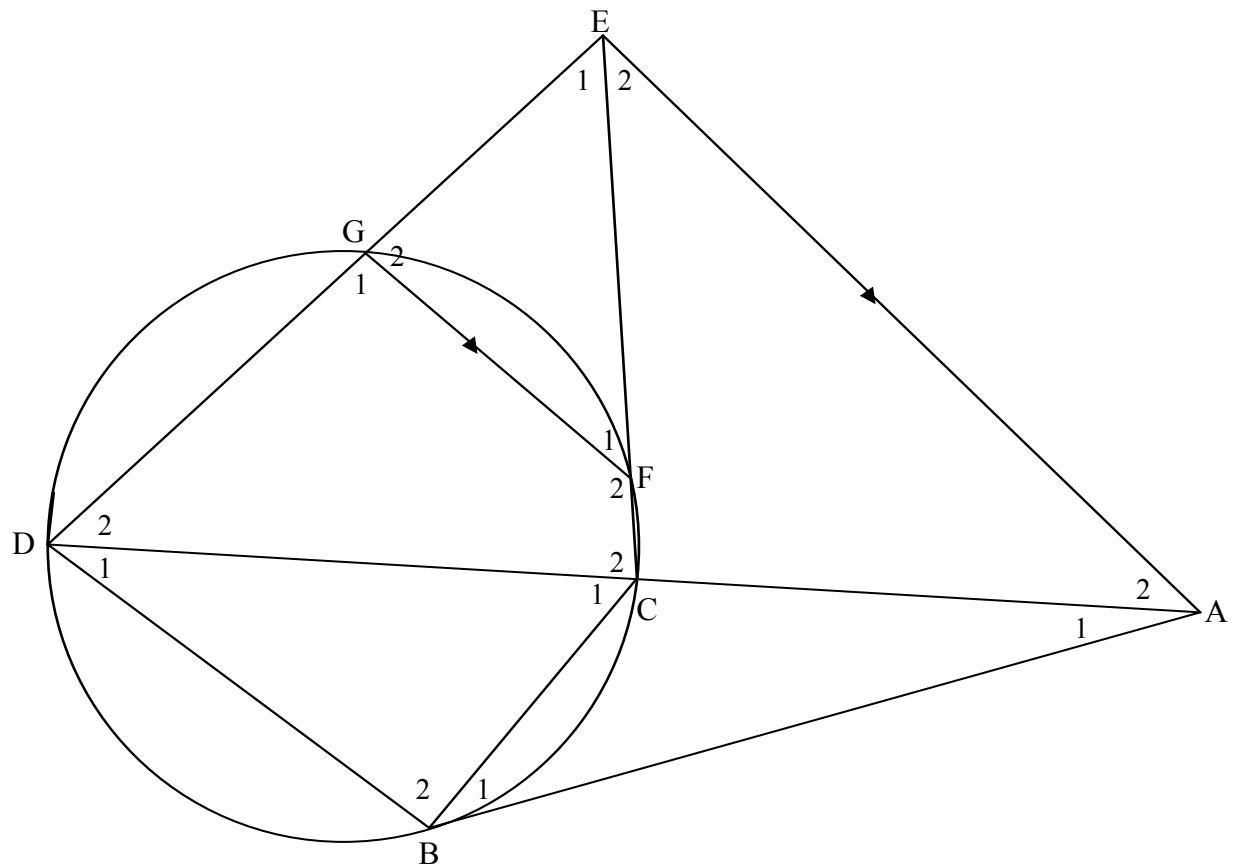


9.1.1	verwiss $\angle e$ /alternate $\angle s$ ; $CD \parallel OA$	$\checkmark R$	(1)
9.1.2	$CO = OA$ [radii] $\angle s$ opp equal sides/ $\angle e$ to gelyke sye	$\checkmark R$	(1)
9.2.1	$\hat{CAB} = 90^\circ$ [ $\angle$ in semi-circle/halfsirkel] $\therefore \hat{A}_1 = 90^\circ - x$	$\checkmark S \checkmark R$ $\checkmark S$	(3)
9.2.2	$\hat{O}_1 = 2x$ [ $\angle$ at centre = $2 \times \angle$ at circum/midpts $\angle$ = $2 \times$ omtr $\angle$ ]	$\checkmark S \checkmark R$	(2)
9.2.3	$\hat{O}_2 = 2x$ [ext $\angle$ of $\Delta ACO$ ] OR $\hat{O}_2 = 2x$ [ $\angle$ at centre = $2 \times \angle$ at circum/midpts $\angle$ = $2 \times$ omtr $\angle$ ] OR $\hat{A}_1 = 90^\circ - x = \hat{B}$ [ $\angle$ s opp equal sides/ $\angle e$ to gelyke sye] $\therefore \hat{O}_2 = 180^\circ - 2(90^\circ - x) = 2x$ [ $\angle$ s of $\Delta$ ]	$\checkmark S \checkmark R$ $\checkmark S \checkmark R$ $\checkmark R$ $\checkmark S$	(2)
9.3	$E\hat{O}B = 4x$ [ $\hat{O}_1 = 2x$ and $\hat{O}_2 = 2x$ ] $E\hat{O}B + E\hat{A}B = 180^\circ$ [opp $\angle$ s of cyc quad supp/ to $\angle e$ v kdvh suppl] $\therefore 4x + 90^\circ = 180^\circ$ $x = 22,5^\circ$	$\checkmark R$ $\checkmark$ equation $\checkmark$ answer	(3)
			[12]

**QUESTION/ VRAAG 10**

10.1	proportional/eweredig	<input checked="" type="checkbox"/> S	(1)
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10.2

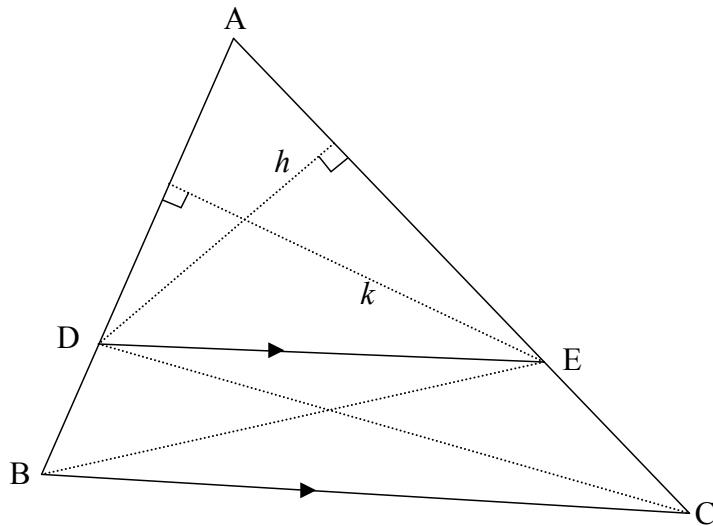


10.2.1	tangent-chord theorem / raaklyn-koordstelling	<input checked="" type="checkbox"/> R	(1)
10.2.2	<p>In <math>\triangle ABC</math> and <math>\triangle ADB</math>:</p> $\hat{A}_1 = \hat{A}_1 \quad [\text{common/gemeenskaplik}]$ $\hat{B}_1 = \hat{D}_1 \quad [\text{proven/bewys in 10.2.1}]$ $\therefore \triangle ABC \parallel \triangle ADB \quad [\angle ; \angle ; \angle]$ <p>OR</p> <p>In <math>\triangle ABC</math> and <math>\triangle ADB</math>:</p> $\hat{A}_1 = \hat{A}_1 \quad [\text{common/gemeenskaplik}]$ $\hat{B}_1 = \hat{D}_1 \quad [\text{proven/bewys in 10.2.1}]$ $\hat{B}_2 = \hat{C} \quad [\angle s \text{ of } \Delta = 180^\circ]$ $\therefore \triangle ABC \parallel \triangle ADB$	<input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> R <input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> R	(3)

10.2.3	$\hat{E}_2 = \hat{F}_1$ [verwiss $\angle e$ /alternate $\angle s$ ; EA    GF] $\hat{F}_1 = \hat{D}_2$ [ext $\angle$ of cyc quad DGFC/buite $\angle v$ kdvh DGFC] $\therefore \hat{E}_2 = \hat{D}_2$	$\checkmark S \quad \checkmark R$ $\checkmark S \quad \checkmark R$	
10.2.4	In $\Delta AEC$ and $\Delta ADE$ : $\hat{A}_2 = \hat{A}_2$ [common/gemeenskaplik] $\hat{E}_2 = \hat{D}_2$ [proven/bewys in 10.2.3] $\therefore \Delta AEC \parallel\parallel \Delta ADE [\angle ; \angle ; \angle]$ $\therefore \frac{AE}{AD} = \frac{AC}{AE}$ $\therefore AE^2 = AD \times AC$ OR In $\Delta AEC$ and $\Delta ADE$ : $\hat{A}_2 = \hat{A}_2$ [common/gemeenskaplik] $\hat{E}_2 = \hat{D}_2$ [proven/bewys in 10.2.3] $A\hat{C}E = \hat{G}_1$ [ $\angle s$ of $\Delta = 180^\circ$ OR ext $\angle$ of cyc quad DGFC/ buite $\angle v$ kdvh DGFC] $\therefore \Delta AEC \parallel\parallel \Delta ADE$ $\therefore \frac{AE}{AD} = \frac{AC}{AE}$ $\therefore AE^2 = AD \times AC$	$\checkmark S$ $\checkmark S$ $\checkmark R$ $\checkmark S$  $\checkmark S$ $\checkmark S$ $\checkmark R$ $\checkmark S$	(4)
10.2.5	$\frac{AB}{AD} = \frac{AC}{AB}$ [ $\Delta ABC \parallel\parallel \Delta ADB$ ] $AB^2 = AD \times AC$ $= AE^2$ [from 10.2.4] $\therefore AB = AE$	$\checkmark S$  $\checkmark S$ $\checkmark S$	(3)
			[16]

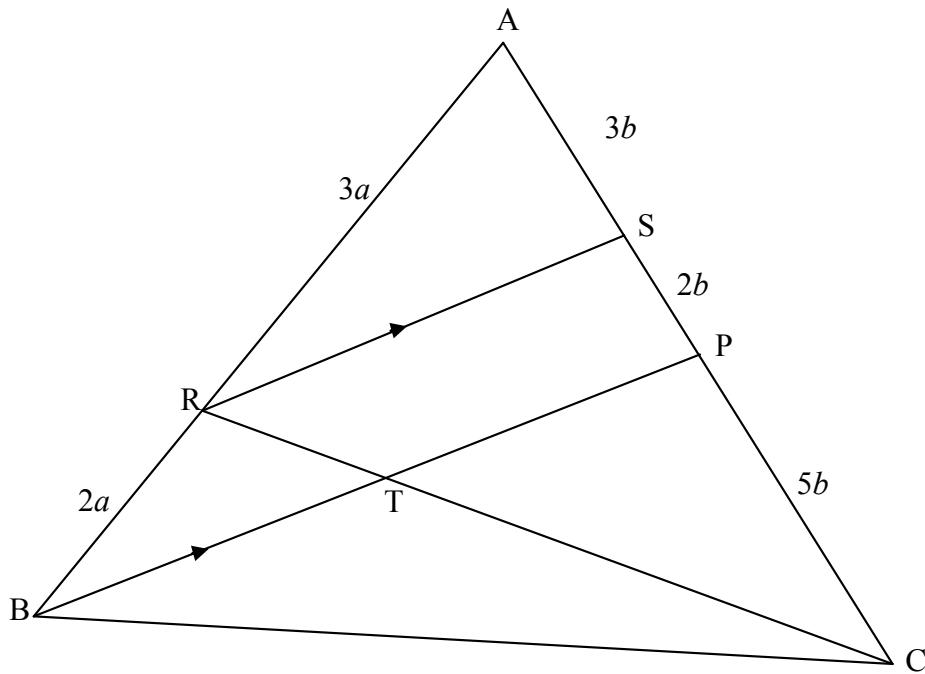
**QUESTION/ VRAAG 11**

11.1



	<p>Construction: Connect DC and BE and draw the altitudes <math>k</math> and <math>h</math>          Konstruksie: Verbind DC en BE en trek hoogtelyne <math>k</math> en <math>h</math>.</p>	✓ constr/ konstr (on sketch or wording/ op skets of beskrywing)	
	$\frac{\text{Area } \Delta ADE}{\text{Area } \Delta BDE} = \frac{\frac{1}{2} \times AD \times k}{\frac{1}{2} \times BD \times k} = \frac{AD}{BD}$ $\frac{\text{Area } \Delta ADE}{\text{Area } \Delta DEC} = \frac{\frac{1}{2} \times AE \times h}{\frac{1}{2} \times EC \times h} = \frac{AE}{EC}$ <p>but/maar: Area <math>\Delta BDE</math> = Area <math>\Delta DEC</math> [DE common base and <math>DE \parallel BC</math>/ DE gemeensk basis en <math>DE \parallel BC</math>]</p> $\therefore \frac{\text{Area } \Delta ADE}{\text{Area } \Delta BDE} = \frac{\text{Area } \Delta ADE}{\text{Area } \Delta DEC}$ $\therefore \frac{AD}{BD} = \frac{AE}{EC}$	✓S ✓S ✓S ✓R ✓conclusion	
			(6)

11.2



11.2.1	$\frac{AS}{SP} = \frac{AR}{RB}$ $= \frac{3}{2}$ $\frac{AS}{SC} = \frac{3}{7}$ [AP = PC]	$\checkmark S \checkmark R$ $\checkmark$ answer $\checkmark S$	(4)
11.2.2	$\frac{RT}{TC} = \frac{SP}{PC}$ $= \frac{2}{5}$ [line    side of $\Delta$ OR RS    TP]	$\checkmark S \checkmark R$ $\checkmark$ answer	(3)
11.2.3	$\frac{\text{Area } \Delta TPC}{\text{Area } \Delta RSC} = \frac{\frac{1}{2} TC \cdot PC \cdot \sin \hat{T}CP}{\frac{1}{2} RC \cdot SC \cdot \sin \hat{T}CP}$ $= \frac{TC}{RC} \times \frac{PC}{SC}$ $= \frac{5}{7} \times \frac{5}{7}$ $= \frac{25}{49}$	$\checkmark$ Correct subst into area rule $\checkmark \frac{5}{7} \checkmark \frac{5}{7}$ $\checkmark$ answer	(4)
			[17]