

$$1.1. \begin{aligned} -18,75 &= a(9,5) + b(-7) \\ 28,375 &= a(-18,75) + b(9,5) \end{aligned}$$

$$\therefore a = -\frac{1}{2} \quad b = 2$$

$$1.2. 9,5 = -\frac{1}{2}(-7) + 2(T_1)$$

$$3 - \cancel{7} = T_1$$

$$2. T_0 = 650$$

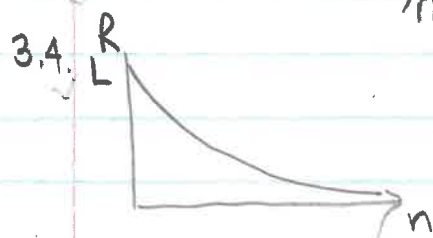
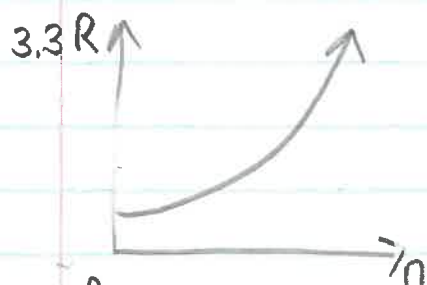
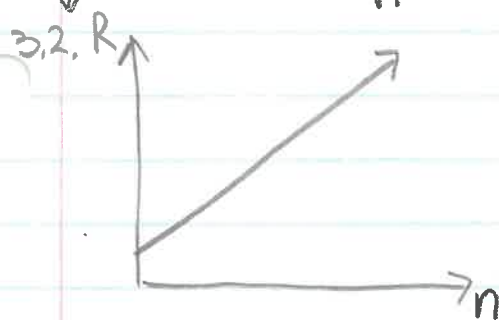
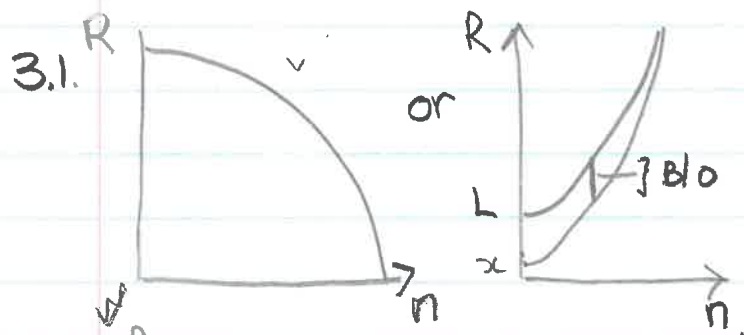
$$T_1 = (1+20\%)T_0 + T_0(1+\frac{18\%}{12})$$

$$T_2 = (1+20\%)(1+20\%)T_0 + T_1(1+\frac{18\%}{12})$$

$$T_3 = (1+20\%)^3 T_0 + T_2(1+\frac{18\%}{12})$$

$$\therefore T_n = (1+20\%)^n T_0 + T_{n-1}(1+\frac{18\%}{12})$$

$$T_0 = 650$$



4.1.

$$\frac{1}{T_0} \quad \frac{1}{T_8} \quad \frac{1}{T_9} \quad \frac{1}{T_{20}} \quad \frac{1}{T_n}$$

$$A = (1 + \frac{9,75\%}{12})$$

$$3 \times 10^6 A^n = \frac{40 \times 10^3 (A^{n-18} - 1)}{A - 1}$$

$$n = 168 \text{ months.}$$

$$\text{ie } 14 \text{ years.}$$

4.2.

$$T_0 \quad T_8 \quad T_9 \quad T_{18} \quad \text{B.O? at } T_8$$

$$B.O = \frac{3 \times 10^6 A^{78} - 40 \times 10^3 (A^{60} - 1)}{A - 1}$$

$$= 2562432,476$$

Invest 1, 2 million

$\therefore 1362432,47$ is in bank.

$$136 \dots \quad 15k \quad T_0 \quad T_1 \quad T_n$$

$$136 \dots A^n = \frac{15k(A^n - 1)}{A - 1}$$

$$n = 165 \text{ months.}$$

$$13 \text{ and } \frac{3}{4} \text{ years.}$$

$$5. P_{n+1} = P_n(1+r)$$

$$5.1. SA: P_{n+1} = P(1+0,0083)$$

$$r = 0,0083 \text{ increasing.}$$

$$G: P_{n+1} = P(1-0,0006)$$

$$r = 0,0006 \text{ decreasing}$$

$$5.2. SA: A = 55\,436\,360(1+0,0083)^n$$

$$G: A = 80\,636\,124(1-0,0006)^n$$

$$n = 42,26 \dots$$

$$\text{ie } n = 43 \text{ years.}$$

6.1. $r = b - d.$

$$b = \text{surv rate} \times \% \text{ fem} \times \text{litter size} \times \text{fert cyc}$$

$$= 70\% \times 55\% \times 3 \times 2/1.$$

$$d = \text{cycle/lifespan}$$

$$= 1/7$$

$$\therefore r = \frac{1517}{700}$$

$$= 2,1671.$$

6.2. $P_{n+1} = P_n(1 + 2,17)$

6.3. $P_0 = 15.$

$$P_1 = 47,55$$

$$P_2 = 150,7335$$

$$P_3 = 477,825..$$

$$P_4 = 1514,705..$$

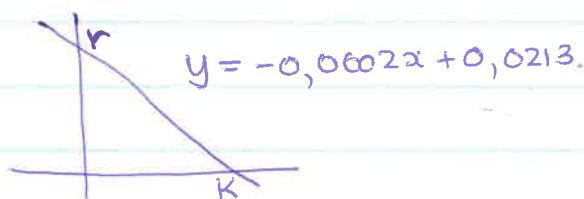
$$P_5 = 4801,617..$$

$$P_6 = 15221,127..$$

$$P_7 = 48250,975..$$

$$\therefore 48250.$$

7.1.



a) $r = 0,0213.$

b) $K = \frac{0,0213}{0,0002} = 106.$

c) $\frac{\Delta P}{P} = -\frac{r}{K} P_n + 6.$

$$= -0,0002(32) + 0,0213$$

$$= 0,0149.$$

d) $P_{n+1} = P_n + r P_n \left(1 - \frac{P_n}{K}\right)$

$$= P_n + 0,0149 P_n \left(1 - \frac{P_n}{106}\right)$$

$$P_0 = 21$$

$$P_1 = 21,25..$$

$$P_2 = 21,504..$$

$$P_3 = 21,759...$$

$$P_4 = 22,017..$$

$$P_5 = 22,277..$$

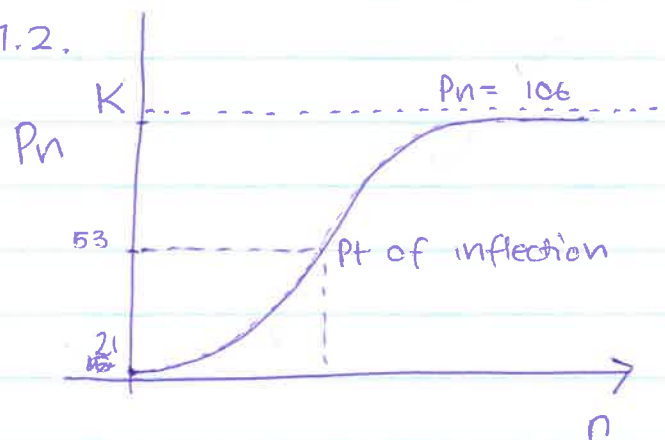
$$P_6 = 22,539..$$

$$P_7 = 22,803..$$

$$P_8 = 23,070$$

ie $P_8 = 23.$

7.2.



8. ~~$P_{n+1} = P_n + a P_n \left(1 - \frac{P_n}{K}\right) - b R_n F_n$~~

8.1. $P_{n+1} = P_n$

8.2. $a \left(1 - \frac{P_n}{K}\right) = b F_n.$

~~$F_{n+1} = F_n + f b R_n F_n - c F_n$~~

~~$F_{n+1} = F_n$~~

$\therefore f b R_n = c.$

$\therefore R_n = \frac{c}{f b}.$

$\therefore a \left(1 - \frac{c}{f b K}\right) = b F_n.$

$\therefore F_n = \frac{a}{b} \left(1 - \frac{c}{f b K}\right)$

9.1. Pred 30 ✓
Prey 70. ✓

9.2. a) Prey ✓
max 500 ✓
min 10

b) Predator ✓
max 50 ✓
min 20.

9.3. Low # predators ✓
∴ ↑ growth rate of ✓
prey.

Some could have been
introduced as it is so
steep.