

GRADE II NOV EXAM PI MEMO

Question 1

d. $x = \frac{8 \pm \sqrt{64 + 36}}{6} \checkmark$
 $= \frac{8 \pm \sqrt{100}}{6} \checkmark$

$x = 3 \checkmark$ or $x = -\frac{1}{3} \checkmark$

bi $16^{-\frac{1}{4}} + (-10)^0$
 $= (2^4)^{-\frac{1}{4}} + 1 \checkmark$
 $= 1\frac{1}{2} \checkmark$

ii $\sqrt[3]{3a^2} \times \sqrt[3]{9a^4}$
 $= \sqrt[3]{27a^6} \checkmark$
 $= 3a^2 \checkmark$

iii $\frac{x^2 + 5x + 6}{3x + 6}$
 $= \frac{(x+2)(x+3)}{3(x+2)} \checkmark$
 $= \frac{x+3}{3} \checkmark$

iv. $\frac{6^{n+2} \times 10^{n-2}}{4^n \times 15^{n-2}}$
 $= \frac{2^{n+2} \cdot 3^{n+2} \times 2^{n-2} \cdot 5^{n-2}}{2^{2n} \times 3^{n-2} \cdot 5^{n-2}} \checkmark$
 $= 2^{n+2+n-2-2n} \cdot 3^{n+2-(n-2)} \cdot 5^{n-2-(n-2)} \checkmark$
 $= 2^0 \cdot 3^4 \cdot 5^0 \checkmark$
 $= 81 \checkmark$

Question 2

2a. $2 \cdot 3^{3x+1} = 162$
 $3^{3x+1} = 81 = 3^4 \checkmark$
 $3x+1 = 4 \checkmark$
 $x = 1 \checkmark$

b. $x^2 - 3x - 6 = 0$
 $x = \frac{3 \pm \sqrt{9 - 4(1)(-6)}}{2} \checkmark$

$x = 4,37 \checkmark$ or $x = -1,37 \checkmark$

c. $2x^{\frac{1}{2}} - 5x^{\frac{1}{4}} - 3 = 0$
 $(2x^{\frac{1}{4}} + 1)(x^{\frac{1}{4}} - 3) = 0$
 $x^{\frac{1}{4}} \neq -\frac{1}{2} \checkmark$ or $x^{\frac{1}{4}} = 3 \checkmark$
 $x = \sqrt[4]{16} \checkmark$ or $x = 81 \checkmark$

d. $\sqrt{x+4} - x = 4$
 $\sqrt{x+4} = x+4 \checkmark$
 $x+4 = x^2 + 8x + 16 \checkmark$
 $0 = x^2 + 7x + 12 \checkmark$
 $(x+3)(x+4) = 0 \checkmark$
 $x = -3 \checkmark$ or $x = -4 \checkmark$

e. $x+2 = \frac{25}{x+2}$
 $x^2 + 4x + 4 = 25 \checkmark$
 $x^2 + 4x - 21 = 0 \checkmark$
 $(x+7)(x-3) = 0 \checkmark$
 $x = -7 \checkmark$ or $x = 3 \checkmark$

f. $x(x-3) \geq -2$
 $x^2 - 3x + 2 \geq 0 \checkmark$
 $(x-2)(x-1) \geq 0 \checkmark$
 $x \leq 1 \checkmark$ or $x \geq 2 \checkmark$

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Question 3

ai $7; 19; 37; 61$
 $\begin{array}{ccc} \underbrace{} & \underbrace{} & \underbrace{} \\ +12 & +18 & +24 \\ \hline & +6 & +6 \end{array}$

$91; 127$

ii. $T_n = ax^2 + bx + c$

$a = \frac{b}{2} = 3$

$b = 12 - 3(3) = 3$

$c = 7 - (3 + 3) = 1$

$T_n = 3x^2 + 3x + 1$

b. $2x + 2 - x = 5x + 3 - (2x + 2)$

$x - 3x = -1$

$-2x = -1$

$x = \frac{1}{2}$

$\frac{1}{2}; 3; 5\frac{1}{2}$

ai $T_n = 1,6n$

$S_{40} = \frac{40}{2} (1,6 + 64) = 1312 \text{ km}$

ii $T_{30} = 1,6(30) = 48 \text{ km}$

di $S_{12} = 3^{13} - 6 = 1594217$

ii $T_{12} = S_{12} - S_{11} = 1594317 - 531435 = 1062882$

iii. $T_n = S_n - S_{n-1} = 3^{n+1} - 6 - (3^n - 6) = 3^{n+1} - 3^n = 3^n(3-1) = 2 \cdot 3^n$

\therefore divisible by 2

Question 4

4di $f(x) = 3x^2 + 6x = 3(x^2 + 2x + (\frac{2}{2})^2 - (\frac{2}{2})^2) = 3[(x+1)^2 - 1] = 3(x+1)^2 - 3$

ii. TP: $(-1; -3)$

min: -3

bi $y = x^2 - 4; 2x = y + 4$

$2x = x^2 - 4 + 4$

$0 = x^2 - 2x$

$0 = x(x-2)$

$x = 0 \text{ or } x = 2$

$y = -4 \text{ or } y = 0$

ii. Answer sheet

$$\text{iii. } y = (x-3)^2 - 4 \\ = x^2 - 6x + 5$$

Question 5

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a. v ✓

b. vi ✓

c. ii ✓

Question 6

a. $p=2$ ✓ $q=1$ ✓

$$f(x) = a(x-2) + 1$$

$$f(3) = a(3-2) + 1 = 3$$

$$a + 1 = 3$$

$$a = 2$$

g) d.

4

b. $x=2$ ✓ $y=1$ ✓

c. $y=x-1$ ✓ or $y=-x+3$ ✓

d. $y \geq 2$ ✓, $y \in \mathbb{R}$ ✓

e. $f(0) = 2(0-2)^2 + 1$ ✓
 $= 9$ ✓

f. $(2; 3]$ ✓

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Question 7

a. $A = P(1-i)^n$ ✓
 $= 24\,000(1-18\%)^3$ ✓
 $= R\,13\,232,83$ ✓ 3

e) b. $i_{\text{eff}} = (1 + \frac{14\%}{12})^{12} - 1$ ✓
 $= 0,1493\dots$ ✓
 $= 14,93\%$ ✓ 3

[37] c.

$$2x = x(1 + 8,5\% \cdot n)$$
 ✓

$$1 + 8,5\% \cdot n = 2$$
 ✓

$$n = \frac{2-1}{8,5\%} = 11,764$$

$$= 12 \text{ years}$$
 ✓ 4

$$A_n = P(1+i)^n$$

$$= 2850(1 + \frac{8\%}{4})^{36}$$
 ✓
$$= R\,5813,68$$
 ✓

$$A_{15} = 5813,68(1 + \frac{10,5\%}{12})^{72}$$
 ✓
$$= R\,10\,885,95$$
 ✓ 6

Question 8

[16]

a. $\frac{550}{1000} = 0,55$ ✓ 2

b. $\frac{450}{600} = 0,75$ ✓ 2

c. $\frac{100}{400} = 0,25$ ✓ [6]

Question 9

a. 14 ✓

1

b. $160 - 24$ ✓ = 136 ✓

2

c. $16 + 22 + 28 + 14$ ✓ = 80 ✓

2

d. $38 - x + x + 34 - x + 80 = 136$

$$-x = -152 + 136$$

$$x = 16$$
 ✓

3

Question 10

[8]

$$C = 2\pi x$$
 ✓

$$\text{Per of square} = 200 - 2\pi x$$

$$\text{Side of square} = 50 - \frac{\pi x}{2}$$
 ✓

Area of square:

$$\begin{aligned} & \left(50 - \frac{\pi x}{2}\right)^2 \checkmark \\ & = 2500 - 50\pi x + \frac{\pi^2 x^2}{4} \end{aligned}$$

[6]

Name: _____

Question 4bi.

