



GAUTENG DEPARTMENT OF EDUCATION

PROVINCIAL EXAMINATION

2016

GRADE 11

**MATHEMATICS
Second Paper**

MEMORANDUM

11 pages

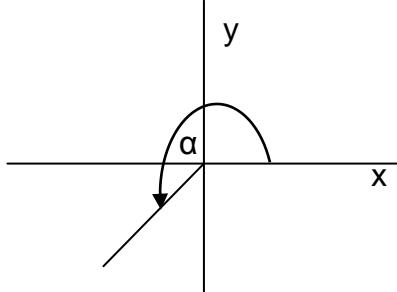
GAUTENG DEPARTMENT OF EDUCATION**PROVINCIAL EXAMINATION****MATHEMATICS
(Second Paper)**

INFORMATION:

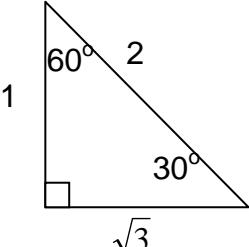
- A – Accuracy
- C.A. – Continued Accuracy
- S – Statement
- R – Reason
- S and R – Statement and Reason

	QUESTION 1	MARKS : 16
1.1	$\begin{aligned} KT &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(-5 - 1)^2 + (1 - 6)^2} \\ &= \sqrt{61} \end{aligned}$	<ul style="list-style-type: none"> ✓ Distance formula ✓ subst. in corr. formula ✓ answer <p>[2/3 if answer not in surd form] (3)</p>
1.2	$\begin{aligned} m_{KP} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= -\frac{1}{4} \end{aligned}$ $(y - y_1) = m(x - x_1)$ $(y - 1) = -\frac{1}{4}(x - (-5))$ $y = -\frac{1}{4}x - \frac{1}{4}$ <p style="text-align: center;">OR</p> $\begin{aligned} m_{KP} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= -\frac{1}{4} \end{aligned}$ $(y - (-2)) = -\frac{1}{4}(x - 7)$ $y = -\frac{1}{4}x - \frac{1}{4}$	<ul style="list-style-type: none"> ✓ answer m_{KP} ✓ subst. (-5 ; 1) into str. line eq. ✓ answer (C.A) <p>OR</p> <ul style="list-style-type: none"> ✓ answer m_{KP} ✓ subst. (7 ;-2) into str. line eq. ✓ answer (C.A) (3)
1.3	$\begin{aligned} m_{KT} &= \frac{6-1}{1-(-5)} \\ &= \frac{5}{6} \end{aligned}$ $(y - 6) = \frac{5}{6}(x - 1)$ $y = \frac{5}{6}x + 5\frac{1}{6}$ <p>A $(0 ; 5\frac{1}{6})$ B $(0 ; -\frac{1}{4})$</p> $\begin{aligned} AB &= 5\frac{1}{6} + \frac{1}{4} \\ &= 5\frac{5}{12} \quad \text{OR } 5,42 \quad \text{OR } \frac{65}{12} \end{aligned}$	<ul style="list-style-type: none"> ✓ answer m_{KT} (A) ✓ eq. of Line KT. (A) OR y-int of line KT. ✓ add of y co-ord. of A and B ✓ answer (A) (4)

1.4	$\tan \beta = \frac{m_{KT}}{5}$ $\tan \beta = \frac{5}{6}$ $\beta = 39,81^\circ$ $m_{PT} = -\frac{4}{3}$ $\tan \alpha = -\frac{4}{3}$ $\alpha = 180^\circ - 53,13^\circ$ $= 126,87^\circ$ $\theta = \alpha - \beta \dots \text{ext. } \angle \text{ of } \Delta$ $= 126,87^\circ - 39,81^\circ$ $= 87,06^\circ$ ANY other valid solution	✓ $\tan \beta = \frac{5}{6}$ ✓ $\beta = 39,81^\circ$ ✓ $\tan \alpha = -\frac{4}{3}$ ✓ $\alpha = 126,87^\circ$ ✓ $126,87^\circ - 39,81^\circ$ ✓ answer (PENALISE once for rounding off, either α or β)
	QUESTION 2	MARKS : 14
2.1	Let M ($x ; y$) $OM^2 = MB^2 \dots \text{radii}$ $(0-x)^2 + (0-y)^2 = (8-x)^2 + (0-y)^2$ $x^2 + y^2 = 64 - 16x + x^2 + y^2$ $x = 4$	✓ $OM^2 = MB^2$ ✓ corr. Subst. in dist. formula ✓ simplification (C.A) ✓ answer (4) Answer only 0
2.2	A($x ; y$) $x = 0$ $\frac{0+y}{2} = 2$ $y = 4$ A(0 ; 4)	✓ subst. in midpt. formula ✓ $y = 0$ ✓ co-ord. of A [2/3 if not in co-ordinate form]
2.3	$m_{AB} = -\frac{1}{2}$ Eq. of line OK: $y - y_1 = m(x - x_1)$ $y - 0 = -\frac{1}{2}(x - 0)$ $y = -\frac{1}{2}x$	✓ m_{AB} ✓ corr. subst. in str. line formula ✓ answer (C.A)

2.4	<p>Let T $(x ; y)$</p> $m_{AT} = \frac{4-y}{-x}$ $\frac{4-y}{-x} \times -\frac{1}{2} = -1 \dots \perp \text{ lines}$ $y = 2x + 4 \dots \text{(1)}$ <p>Eq. of line OK</p> $y = -\frac{1}{2}x \dots \text{(2)}$ $2x + 4 = -\frac{1}{2}x$ $x = -\frac{8}{5}$ <p>Any other valid method</p>	$\checkmark \frac{4-y}{-x} \times -\frac{1}{2} = -1$ $\checkmark y = 2x + 4$ \checkmark equating (1) and (2) \checkmark answer (C.A)
	QUESTION 3	MARKS 28
3.1	<p>$13\sin\alpha = -5$</p> $\sin\alpha = -\frac{5}{13}$  $x = -\sqrt{13^2 - (-5)^2}$ $= -12$ <p>$3\cos\alpha$</p> $= 3\left(-\frac{12}{13}\right)$ $= -\frac{36}{13}$	$\checkmark \sin\alpha = -\frac{5}{13}$ \checkmark cartesian plane with terminal arm in 3rd quad. $\checkmark x = -12$ \checkmark subst. $\cos\alpha = -\frac{12}{13}$ \checkmark answer

3.2.1	$\frac{\sin(\theta - 180^\circ) \cdot \tan(360^\circ - \theta) \cdot \sin(90^\circ - \theta)}{\cos^2(\theta + 180^\circ)}$ $= \frac{-\sin \theta \times -\tan \theta \times \cos \theta}{\cos^2 \theta}$ $= \frac{-\sin \theta \times -\frac{\sin \theta}{\cos \theta} \times \cos \theta}{\cos^2 \theta}$ $= \frac{\sin^2 \theta}{\cos^2 \theta}$ $= \tan^2 \theta$	✓ -sin θ ; ✓ -tan θ ; ✓ cos θ ; ✓ $\cos^2 \theta$ ✓ -tan $\theta = -\frac{\sin \theta}{\cos \theta}$ ✓ $\frac{\sin^2 \theta}{\cos^2 \theta}$ or tan $^2 \theta$ (6)
3.2.2	$\frac{\sin 210^\circ \cdot \cos 400^\circ}{\sin(-50^\circ) \times \cos 120^\circ}$ $= \frac{\sin(180^\circ + 30^\circ) \times \cos(360^\circ + 40^\circ)}{-\sin 50^\circ \times \cos(180^\circ - 60^\circ)}$ $= \frac{-\sin 30^\circ \times \cos 40^\circ}{-\cos 40^\circ \times -\cos 60^\circ}$ $= -1$	✓ -sin 50 $^\circ$ ✓ - sin 30 $^\circ$; ✓ cos 40 $^\circ$; ✓ - cos 40 $^\circ$ or cos 40 $^\circ$ = sin 50 $^\circ$ ✓ - cos 60 $^\circ$ ✓ answer (6)
3.3	$(4\theta - 8) \sin 30^\circ = \theta^3 - 8$ $(4\theta - 8) \sin 30^\circ = (\theta - 2)(\theta^2 + 2\theta + 4)$ $(4\theta - 8) \sin 30^\circ = (\theta - 2)(2)$ $\sin 30^\circ = \frac{(\theta - 2)(2)}{(4\theta - 8)}$ $= \frac{(\theta - 2)(2)}{4(\theta - 2)}$ $= \frac{1}{2}$	✓ factorization ✓ factorization of denominator ✓ answer

	 <p>$\tan 240^\circ = \tan (180^\circ + 60^\circ)$ $= \tan 60^\circ$ $= \sqrt{3}$</p>	<ul style="list-style-type: none"> ✓ $\tan 60^\circ$ ✓ answer <p>Full marks if $\tan 60^\circ = \sqrt{3}$ or Show sketch to determine sol. Answer only max 1 mark(surd form)</p>
3.4.1	<p>L.H.S: $\frac{1}{\tan x} (\sin \alpha \tan \alpha + \cos \alpha)$</p> $= \sin \alpha + \frac{\cos \alpha}{\tan \alpha}$ $= \sin \alpha + \frac{\cos \alpha}{\frac{\sin \alpha}{\cos \alpha}}$ $= \sin \alpha + \frac{\cos^2 \alpha}{\sin \alpha}$ $= \frac{\sin^2 \alpha + \cos^2 \alpha}{\sin \alpha}$ $= \frac{1}{\sin \alpha} = \text{R.H.S}$ <p>Any other valid method</p>	<ul style="list-style-type: none"> ✓ $\sin \alpha + \frac{\cos \alpha}{\tan \alpha}$ ✓ subst. $\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$ ✓ $\frac{\cos^2 \alpha}{\sin \alpha}$ ✓ $\frac{\sin^2 \alpha + \cos^2 \alpha}{\sin \alpha}$
3.4.2	$\alpha = \{0^\circ; 90^\circ; 180^\circ; 270^\circ; 360^\circ\}$	<ul style="list-style-type: none"> ✓ $0^\circ; 180^\circ; 360^\circ$ ✓ $90^\circ; 270^\circ$

	QUESTION 4	MARKS 12
4.1	180°	✓ answer (1)
4.2	$y \in [-1; 1]$ OR $-1 \leq y \leq 1, y \in \mathbb{R}$	✓ -1 ;1 ✓ corr. brackets OR ✓ -1 ;1 ✓ corr. inequalities (2)
4.3	$\theta = 40^\circ$ $a = 2$	✓ 40° ✓ 2 (2)
4.4	$g(180^\circ) = -0,77$	✓ answer (C.A) (1)
4.5.1	$f(x) - g(x) > 0$ $f(x) > g(x)$ $-180^\circ \leq x < -103,3^\circ$ OR $[-180^\circ; -103,3^\circ)$	✓ $-180^\circ; -103,3^\circ$ ✓ corr. inequality OR corr. bracket OR $(16,7^\circ; 130^\circ)$ or $(136,7^\circ; 180^\circ]$ (2)
4.5.2	$g(x) \cdot f(x) \geq 0$ $[-130^\circ; -90^\circ]$ OR $-130^\circ \leq x \leq -90^\circ$	✓ $[-130^\circ; -90^\circ]$ ✓ corr brackets OR corr. inequalities $[0^\circ; 50^\circ]$ or $[90^\circ; 180^\circ]$ (2)
4.6	$3^{\cos(90^\circ - 2x)}$ $= 3^{\sin 2x}$ $= 3^{-1}$ OR $= \frac{1}{3}$	✓ $3^{\sin 2x}$ ✓ answer (2)

	QUESTION 5	MARKS 8
5.1	is perpendicular to the chord	✓ answer (1)
5.2.1	$AD = \sqrt{AB^2 + BD^2}$... th. of pyth. $= \sqrt{24^2 + 16^2}$ $= 28,84 \text{ cm}$	✓ Subst. ✓ answer (2)
5.2.2	$OD = x + 16$	✓ answer (1)
5.2.3	$OC^2 = BC^2 + OB^2$ th. of pyth $OD^2 = 24^2 + x^2$ $(x + 16)^2 = 24^2 + x^2$ $x^2 + 32x + 256 = 576 + x^2$ $32x = 320$ $x = 10$	$OC^2 = BC^2 + OB^2$ $OC = OD$ radii ✓ $(x + 16)^2$ ✓ $24^2 + x^2$ ✓ simplification ✓ answer (4)
	QUESTION 6	MARKS 8
6.1	$PT = \frac{1}{2} KT$ line from centre \perp to ch.	✓ S ✓ R (2)
6.2	$KC^2 = PC^2 + KP^2$ th. of pyth. but $KP^2 = OK^2 - OP^2$ th. of pyth. $KC^2 = PC^2 + OK^2 - OP^2$ but $OK = OC$ radii $= PC^2 + OC^2 - (OC - PC)^2$ $= PC^2 + OC^2 - (OC^2 - 2OC \cdot PC + PC^2)$ $= 2(OC \cdot PC)$ $= 2(x + y)(y)$ $= 2xy + 2y^2$	✓ S ✓ $KP^2 = OK^2 - OP^2$ ✓ subst. $OK = OC$ ✓ subst. $OP = OC - PC$ ✓ simplification ✓ subst. for OC and PC (6)

	QUESTION 7	MARKS 14
7.1	$\widehat{U} = \frac{1}{2} V\widehat{S}R \dots\dots \angle \text{ at centre} = 2 \times \angle \text{ on circum.}$ $= \frac{1}{2} (110^\circ)$ $= 55^\circ$	✓ Reason ✓ answer (2)
7.2	$\widehat{V}_2 = \frac{180^\circ - V\widehat{S}R}{2} \dots\dots \angle \text{s opp} = \text{sides, radii}$ $= \frac{180^\circ - 110^\circ}{2}$ $= 35^\circ$	✓ S ✓ R ✓ answer Answer with reason full marks (3)
7.3	$\widehat{R}_2 = (\widehat{R}_3 + \widehat{R}_2) - \widehat{R}_3 \quad \angle \text{s opp} = \text{sides}$ $\widehat{R}_2 = 35^\circ - 20^\circ$ $= 15^\circ$ $\widehat{Q} = \widehat{R}_2 + \widehat{R}_1 \dots\dots \angle \text{s in same seg}$ $= 15^\circ + 30^\circ$ $= 45^\circ$	✓ answer $\widehat{R}_2 = 15^\circ$ ✓ S and R ✓ answer (3)
7.4	$\widehat{K}_4 = \widehat{K}_2 \dots\dots \text{vert opp. } \angle \text{s}$ $= 90^\circ$ $\widehat{P} = 180^\circ - (\widehat{Q} + \widehat{K}_4) \dots\dots \angle \text{s of a } \Delta$ $= 180^\circ - (45^\circ + 90^\circ)$ $= 45^\circ$ OR $\widehat{T} = 180^\circ - (\widehat{K}_2 + \widehat{TRK}) \dots\dots \angle \text{s of a } \Delta$ $= 180^\circ - (90^\circ + 45^\circ)$ $= 45^\circ$ $\widehat{P} = \widehat{T} \dots\dots \angle \text{s in the same seg.}$ $= 45^\circ$	✓ S and R ✓ answer ✓ S and R ✓ answer OR ✓ S and R ✓ answer ✓ S and R ✓ answer (4)

7.5	$\hat{T} = 45^\circ$ $\hat{T} = \hat{Q} = 45^\circ$ $\therefore TR \parallel PQ \dots\dots \text{alt. } \angle s =$ OR $T\hat{R}P = 45^\circ$ $T\hat{R}P = \hat{P} = 45^\circ$ $\therefore TR \parallel PQ \dots\dots \text{alt. } \angle s =$	$\checkmark \hat{T} = 45^\circ$ $\checkmark R$ OR $\checkmark T\hat{R}P = \hat{P}$ $\checkmark R$	(2)
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