

MATHEMATICS
MARKING GUIDELINES

1.	D
2.	C
3.	C
4.	C
5.	C
6.	A
7.	A
8.	B
9.	C
10.	B
11.	D
12.	D
13.	C
14.	D
15.	A
16.	B
17.	C
18.	D
19.	C
20.	D

21.	C
22.	D
23.	B
24.	B
25.	B
26.	D
27.	A
28.	D
29.	A
30.	D
31.	A
32.	D
33.	D
34.	C
35.	C
36.	A
37.	B
38.	A
39.	B
40.	B

QUESTION 1

Answer: (D)

QUESTION 2

Answer: (C)

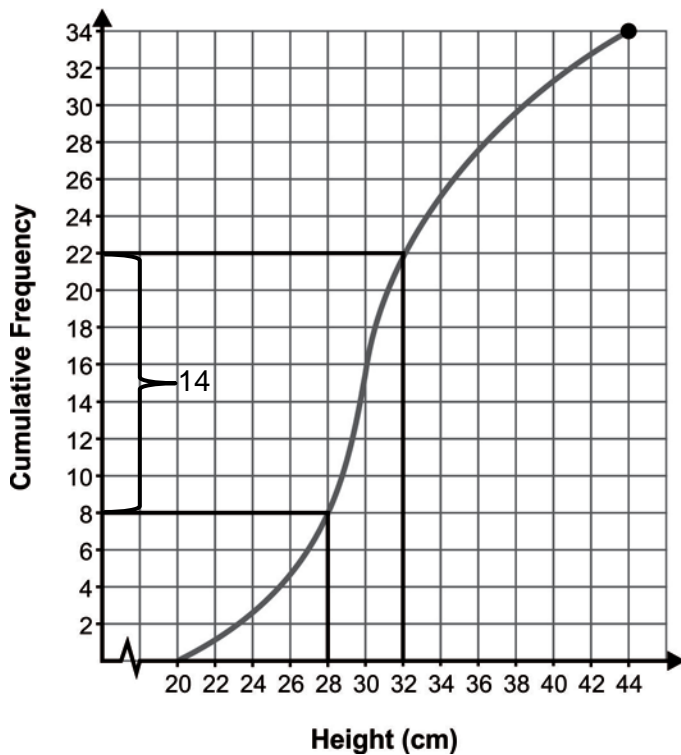
- A False IQR Season 1 < IQR Season 2.
- B False
- C True
- D False, 75% of points for Season 1 were below 25 points

QUESTION 3

Answer: (C)

QUESTION 4

Answer: (C)



QUESTION 5

Answer: (C)

$$x^2 - 6x + 9 - 9 + 3 = 0$$

$$(x - 3)^2 - 6 = 0$$

$$(x - 3)^2 = 6$$

QUESTION 6**Answer: (A)**

$$(5\sqrt{2})^2 = (-2 - (-3))^2 + (y - 4)^2$$

$$50 = 1 + y^2 - 8y + 16$$

$$0 = y^2 - 8y - 33$$

$$0 = (y - 11)(y + 3)$$

$$y = 11 \text{ or } y = -3$$

QUESTION 7**Answer: (A)**

Two periods of compound growth.

QUESTION 8**Answer: (B)**

$$y = \frac{1}{3}x + c$$

$$0 = \frac{1}{3}(7) + c \quad c = \frac{-7}{3}$$

$$y = \frac{1}{3}x - \frac{7}{3}$$

$$3y = x - 7$$

$$3y + 7 = x$$

QUESTION 9**Answer: (C)**

$$A = 3^9 \times 3^8 = 3^{17}$$

$$B = 3^7 \times 3^{12} = 3^{19}$$

$$C = 3^{28} \div 3^8 = 3^{20}$$

$$D = 3^{12} \times 3^6 = 3^{18}$$

QUESTION 10**Answer: (B)**

$$= \frac{\sin x \cdot \sin x}{-\tan x \cdot \cos^2 x}$$

$$= \frac{\sin^2 x}{-\tan x \cdot \cos^2 x}$$

$$= \frac{\tan^2 x}{-\tan x}$$

$$= -\tan x$$

QUESTION 11**Answer: (D)**

Each toss is independent of the tosses before it.

The Answerwer can also be demonstrated using a tree diagram.

QUESTION 12**Answer: (D)**

$$\frac{x}{6} = 50 \quad x = 300$$

$$\frac{300 - 75}{5} = 45$$

QUESTION 13**Answer: (C)**

$$A \quad \frac{\sqrt{12}}{3} \times \frac{\sqrt{12}}{\sqrt{12}} = \frac{12}{3\sqrt{12}} = \frac{4}{\sqrt{12}}$$

$$B \quad \frac{2\sqrt{3}}{3} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{2 \times 3}{3\sqrt{3}} = \frac{2}{\sqrt{3}} \times \frac{2}{2} = \frac{4}{2\sqrt{3}} = \frac{4}{\sqrt{12}}$$

C Incorrect

$$D \quad \frac{2}{\sqrt{3}} \times \frac{2}{2} = \frac{4}{2\sqrt{3}} = \frac{4}{\sqrt{12}} t$$

QUESTION 14**Answer: (D)**

2; 4; 6; 10; 10

Mean = 6.4

SD = 3.2

6; 8; 10; 14; 14

Mean = 10.4

SD = 3.2

Mean will increase with 4 and SD will stay the same

QUESTION 15**Answer: (A)**

$$2^x 5^y = 2^3 \times 2^8 \times 5^8$$

$$2^x 5^y = 2^{11} \times 5^8$$

$$\therefore x = 11 \text{ and } y = 8$$

$$\therefore x - y = 3$$

QUESTION 16**Answer: (B)**

$$\hat{ACD} = 30^\circ \text{ (isos } \Delta)$$

$$\frac{AC}{\sin 120^\circ} = \frac{10}{\sin 30^\circ}$$

$$AC = \frac{\sin 60^\circ \cdot 10}{\sin 30^\circ}$$

$$AC = \frac{\frac{\sqrt{3}}{2} \cdot 10}{\frac{1}{2}}$$

$$AC = 10\sqrt{3}$$

QUESTION 17

Answer: (C)

$$x^2 - 9 = x + 3$$

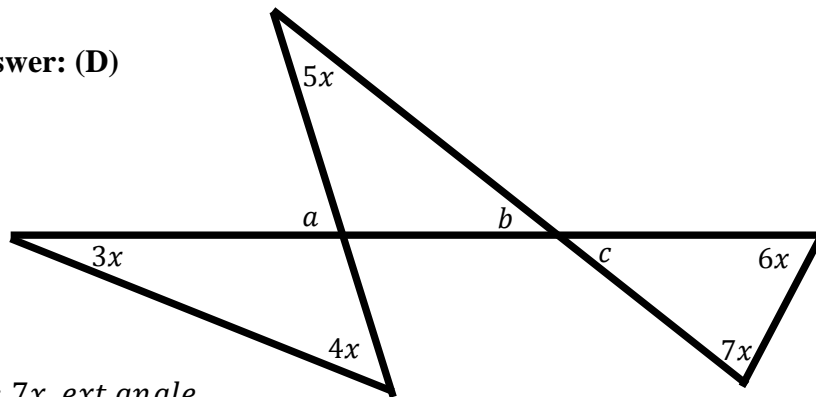
$$x^2 - x - 12 = 0$$

$$(x + 3)(x - 4) = 0$$

$$x = -3 \text{ or } x = 4$$

QUESTION 18

Answer: (D)



$a = 7x$ ext angle
 $b = 2x$ ext angle
 $c = 2x$ vert opp angles
 $2x + 6x + 7x = 180^\circ$ angle sum Δ
 $x = 12^\circ$

QUESTION 19

Answer: (C)

$$f(1) = 9 \left(\frac{4}{3}\right)^1 = 12 \quad f(0) = 9 \left(\frac{4}{3}\right)^0 = 9$$

QUESTION 20

Answer: (D)

$\hat{C}B = 90^\circ$ (\angle in semi circle)
 $\hat{A}BC = 60^\circ$ (int \angle 's of Δ)
 $\hat{D}AC = 60^\circ$ (tan chord theorem)
 $DA = DC$ (tangents from common pt)
 $\hat{D}CA = 60^\circ$ (= \angle 's opp = sides)
 $\hat{ADC} = 60^\circ$ (int \angle 's of triangle)

QUESTION 21**Answer: (C)**

$$\begin{aligned}
&= \frac{\frac{a}{b} - \frac{b}{a}}{\frac{1}{a} + \frac{1}{b}} \\
&= \frac{\frac{a^2 - b^2}{ab}}{\frac{b + a}{ab}} \\
&= \frac{(a + b)(a - b)}{(b + a)} \\
&= \mathbf{a - b}
\end{aligned}$$

QUESTION 22**Answer: (D)**

$$DO = OC(\text{radii})$$

$$O\hat{D}C = O\hat{C}D (= \angle's \text{ opp} = \text{sides})$$

$$C\hat{D}B = C\hat{B}D = \frac{180^\circ - 110^\circ}{2} = 35^\circ (\text{int } \angle's \text{ of triangle})$$

$$\hat{A} + \hat{C} = 180^\circ (\text{opp angles of cyclic quad})$$

$$\hat{A} = 180^\circ - 65^\circ - 35^\circ$$

$$\hat{A} = 80^\circ$$

QUESTION 23**Answer: (B)**

From the graph we have:

$$(x + 1)(x - 4) \leq 0$$

$$x^2 - 3x - 4 \leq 0$$

$$x^2 \leq 3x + 4$$

$$\mathbf{3x + 4 \geq x^2}$$

QUESTION 24**Answer: (B)****Amplitude is 3**Cosine graph moved to the right by 20° .

$$f(x) = 3 \cos(x + (-20^\circ))$$

Sine graph reflected around the x -axis and amplitude is 1, thus $c = -1$ **QUESTION 25****Answer: (B)**

Long method: Solve the quadratic equation to get roots equal to 8 and 1. Substitute either of them into the expression.

Short method: The expression becomes: $x^2 - 9x + 20$
 Which can be written as: $(x^2 - 9x + 8) + 12$
 Which $= 12$ since $x^2 - 9x + 8 = 0$

QUESTION 26**Answer: (D)**

$$2\cos^2 x + \cos x - 1 = 0$$

$$(\cos x + 1)(2\cos x - 1) = 0$$

$$\cos x = -1 \text{ or } \cos x = \frac{1}{2}$$

$$x = 180^\circ + K.360^\circ$$

$$x = 60^\circ + K.360^\circ$$

$$x = 300^\circ + K.360^\circ$$

QUESTION 27**Answer: (A)**

$$\frac{f(x+1)}{f(x)+2} = \frac{2(x+1)}{2x+2} = 1$$

QUESTION 28**Answer: (D)**Here $f(x) \leq g(x)$ and $f(x) \leq 0$ and $g(x) \geq 0$.

QUESTION 29**Answer: (A)**

$$g(x) = f(-x) = \frac{-3}{(-x)+2} - 5 = \frac{3}{x-2} - 5$$

QUESTION 30**Answer: (D)**

Equilateral triangle ABC thus all angles are 60°

$$\begin{aligned} \text{area} &= \frac{1}{2} \cdot 8.8 \cdot \sin 60^\circ \\ &= 32 \cdot \frac{\sqrt{3}}{2} \\ &= 16\sqrt{3} \end{aligned}$$

QUESTION 31**Answer: (A)**

- B Compound interest must be multiplied rather than added
- C This is the return on two separate amounts of R10 000 being invested.
- D Only the compound interest must be multiplied, not the capital invested.

QUESTION 32**Answer: (D)**

$$\tan \theta = \frac{-1}{\sqrt{3}}$$

$$\theta = 30^\circ$$

$$B\hat{A}C = 180^\circ - 45^\circ (\text{vert opp angles}) - 30^\circ (\text{Int. angles of } \Delta)$$

$$B\hat{A}C = 105^\circ$$

QUESTION 33**Answer: (D)**

$$f(x) = \frac{(x+1)+2}{x+1}$$

$$= 1 + \frac{2}{x+1} \text{ So vertical asymptote at } x = -1 \text{ and horizontal asymptote at } y = 1$$

QUESTION 34**Answer: (C)**

$$B\left(\frac{-1+5}{2}; \frac{2+18}{2}\right) \quad B(2; 10)$$

$$BS = \sqrt{(5-2)^2 + (10-10)^2}$$

$$BS = 3$$

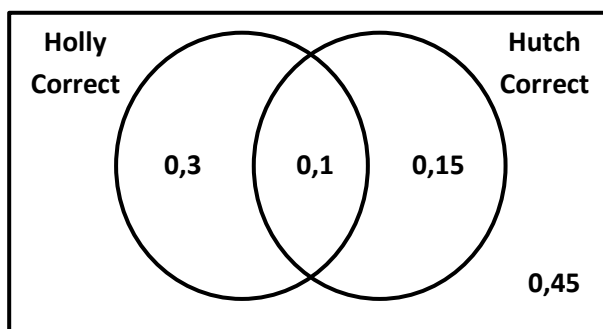
$$\frac{TB}{BS} = \frac{3}{2} \quad \frac{TB}{3} = \frac{3}{2} \quad TB = \frac{9}{2}$$

QUESTION 35**Answer: (C)**

The events are independent, so

$$P(\text{Holly correct}) \times P(\text{Hutch correct}) = 0,4 \times 0,25 = 0,1$$

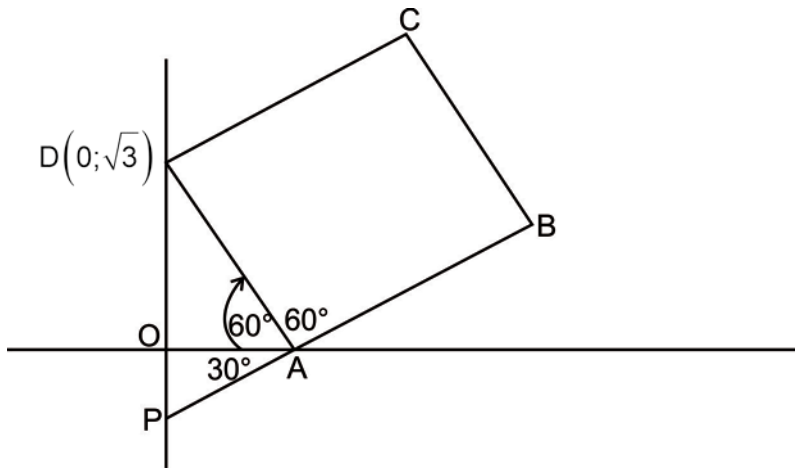
This results in the following Venn Diagram:



The probability that only one of them gets it correct is: $0,3 + 0,15 = 0,45$

QUESTION 36

Answer: (A)



$$\tan 60^\circ = \frac{\sqrt{3}}{OA}$$

$$P\hat{A}O = 30^\circ \text{ (angles on a straight line)}$$

$$PD = \sqrt{3} + \frac{1}{\sqrt{3}}$$

$$\sqrt{3} \cdot OA = \sqrt{3}$$

$$\tan 30^\circ = \frac{OP}{1}$$

$$PD = \frac{4}{\sqrt{3}}$$

$$OA = 1$$

$$\frac{1}{\sqrt{3}} = OP$$

QUESTION 37

Answer: (B)

Expanding the two expressions and setting them equal to each other:

$$f(x) = g(x)$$

$$a(x^2 - 4x + 4) + c = 2x^2 - (5 + 2b)x + 5b$$

$$ax^2 - 4ax + (4 + c) = 2x^2 - (5 + 2b)x + 5b$$

$$\therefore a = 2$$

$$4a = 5 + 2b$$

$$4(2) = 5 + 2b$$

$$b = \frac{3}{2}$$

QUESTION 38

Answer: (A)

$$E\hat{C}G = D\hat{E}C \text{ (alt angles } CG//DE)$$

$$C\hat{E}G = 120^\circ \text{ (int angles of triangle)}$$

$$E\hat{D}C = 120^\circ \text{ (Tan chord theorem)}$$

$$C\hat{B}E = 60^\circ \text{ (opp. angle of cyclic quad)}$$

$$E\hat{B}A = 28^\circ \text{ (angles in same segment)}$$

$$C\hat{B}A = 88^\circ$$

QUESTION 39

Answer: (B)

T_1	T_2	T_3	T_4	T_5
1	3	x	1	y
1 st diff	2	$x - 3$	$1 - x$	$y - 1$
2 nd diff	$x - 5$	$4 - 2x$	$x + y - 2$	

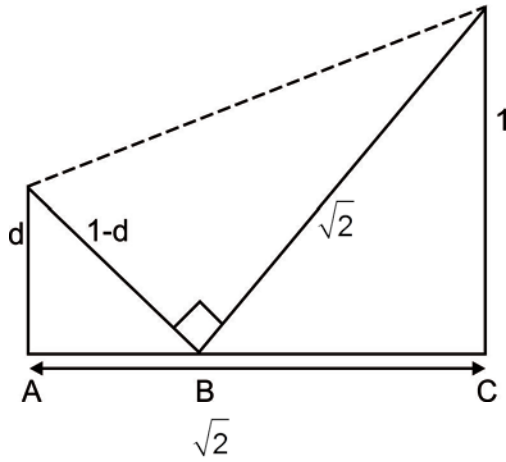
$$x - 5 = 4 - 2x$$

$$x = 3$$

$$x - 5 = x + y - 2$$

$$y = -3$$

$$T_3 + T_5 = x + y = 0$$

QUESTION 40**Answer: (B)**

$$BC^2 = (\sqrt{2})^2 - 1$$

$$BC = \sqrt{2 - 1}$$

$$BC = 1$$

$$AB = \sqrt{2} - 1$$

$$(\sqrt{2} - 1)^2 + (d)^2 = (1 - d)^2$$

$$2 - 2\sqrt{2} + 1 + d^2 = 1 - 2d + d^2$$

$$2 - 2\sqrt{2} = -2d$$

$$-1 + \sqrt{2} = d$$