

Grade 12 Mathematics Paper I Memo 2017

Section A

1) $20x^2 - 50x - 12 = 0$
 $(20x + 3)(x - 4) = 0$
 $x = -\frac{3}{2}$ or $x = 4$ (3)

2) $2\sqrt{x} = 8 - x$
 $4x = 64 - 16x + x^2$
 $0 = x^2 - 20x + 64$
 $0 = (x - 4)(x - 16)$
 $x = 4$; $x \neq 16$ (5)

3) $9x^2 - (2x + 4) > 32x$
 $9x^2 - 15x + 4 > 0$
 $(3x - 1)(3x - 4) > 0$
 $\frac{CVS}{\frac{1}{3}} \quad \frac{1}{3} \quad \frac{4}{3}$
 $x < \frac{1}{3}$ or $x > \frac{4}{3}$ (5)

b) $y = x + 4$
 $x + 4 = 2x^2 + 6x - 8$
 $0 = 2x^2 + 5x - 12$
 $0 = (2x - 3)(x + 4)$
 $x = \frac{3}{2}$ or $x = -4$
 $\therefore y = \frac{5}{2}$ or $y = 0$ (6)

c) $5^x = 2$ and $5^y = 3$ (2)

2) $5^{3x} + 5^{2y}$
 $= (5^x)^3 + (5^y)^2$
 $= 2^3 + 3^2$
 $= 17$ (3)

2a) $p = -13$ (1)

2) $-1 \quad -7 \quad -11 \quad -13$
 $-6 \quad -4 \quad -2$
 $2 \quad 2$

$2a = 2$
 $\therefore a = 1$
 $3a + b = -6$
 $3 + b = -6$
 $b = -9$
 $a + b + c = -1$
 $1 - 9 + c = -1$
 $c = 7$

$\therefore T_n = n^2 - 9n + 7$ (4)

b) $2x + 1 - (2 + x) = x + 4 - (2x + 1)$
 $x - 1 = -x + 3$
 $2x = 4$
 $x = 2$
 $\therefore 4; 5; 6 \dots$
 $\therefore d = 1$ (4)

2c) $r = 2$; $S_6 = -3$
 $a(2^6 - 1) = -3$
 $2 - 1$
 $a = \frac{-3}{63}$
 $a = -\frac{1}{21}$

d) $= \frac{x^2 + x}{x}$
 $r = x + 1$
 $\therefore -1 < x + 1 < 1$
 $-2 < x < 0$ (2)

2) $S_{10} = \frac{x}{1 - (x + 1)}$
 $= -1$ (2)

3a) $85\% \times R800\,000$
 $= R680\,000$
 $680\,000 = x \left[1 - \left(1 + \frac{9.5\%}{12} \right)^{-240} \right]$
 $x = \frac{680\,000 \times \frac{9.5\%}{12}}{\left[1 - \left(1 + \frac{9.5\%}{12} \right)^{-240} \right]}$
 $x = R6338,49$ (5)

b) $R6338,49 \times 240 + R120\,000$
 $= R1\,641\,237,60$ (2)

c) $b = 6338,49 \left[1 - \left(1 + \frac{9.5\%}{12} \right)^{-18} \right]$
 $\frac{9.5\%}{12}$
 $= R566\,659,00$ (3)

d) Amount paid
 $= R6338,49 \times 84$
 $= R532\,433,16$
 Portion of loan paid
 $= R680\,000 - 566\,695$
 $= R113\,305$
 $\therefore \text{Interest} = R419\,128,16$ (4)

4a) $f(x) = a \cdot b^x$
 $1 = a \cdot b^0$
 $\therefore a = 1$
 $\frac{9}{4} = b^2$
 $\therefore b = \frac{3}{2}$
 $f(x) = \left(\frac{3}{2} \right)^x$ (3)

b) $4 = \left(\frac{3}{2} \right)^{4d}$
 $\log 4 = d \cdot \log \frac{3}{2}$
 $\frac{\log 4}{\log \left(\frac{3}{2} \right)} = d$
 $d = 3,4$ (3)

c) $h(x) = -\left(\frac{2}{3} \right)^x$ (1)

d) $y < 0$ (1)

e) $g(x) = \log_{\frac{3}{2}} x$ (2)

3

$$\begin{aligned}
 a) f(x) &= -\frac{1}{2}x^2 + 2x \\
 f(x+h) &= -\frac{1}{2}(x+h)^2 + 2(x+h) \\
 \therefore \Delta f &= \lim_{h \rightarrow 0} \frac{-\frac{1}{2}(x^2 + 2xh + h^2) + 2x + 2h - (-\frac{1}{2}x^2 + 2x)}{h} \\
 &= \lim_{h \rightarrow 0} \frac{-\frac{1}{2}x^2 - xh - \frac{1}{2}h^2 + 2x + 2h + \frac{1}{2}x^2 - 2x}{h} \\
 &= \lim_{h \rightarrow 0} \frac{-xh - \frac{1}{2}h^2 + 2h}{h} \\
 &= \lim_{h \rightarrow 0} (-x - \frac{1}{2}h + 2)
 \end{aligned}$$

$$f'(x) = -x + 2$$

$$\begin{aligned}
 b) y &= 3x^2 + 4x^{\frac{1}{2}} + \frac{8}{3}x^{-2} \\
 \frac{dy}{dx} &= 6x + 2x^{-\frac{1}{2}} - \frac{16}{3}x^{-3} \\
 &= 6x + \frac{2}{x^{\frac{1}{2}}} - \frac{16}{3x^3}
 \end{aligned}$$

$$\begin{aligned}
 c) f(x) &= 4x^3 + px^2 + 4x + p \\
 f'(x) &= 12x^2 + 2px + 4
 \end{aligned}$$

SECTION B

$$\begin{aligned}
 6a) f(x) &= x^3 - 8 \\
 0 &= x^3 - 8 \\
 x^3 &= 8 \\
 x &= 2
 \end{aligned}$$

$$\begin{aligned}
 \therefore P(2; 0) \\
 f'(x) &= 3x^2 \\
 f'(2) &= 3(2)^2 \\
 &= 12
 \end{aligned}$$

$$\begin{aligned}
 \therefore y &= 12x + c \\
 0 &= 12(2) + c \\
 -4 &= c \\
 y &= 12x - 4
 \end{aligned}$$

$$\begin{aligned}
 b) f(x) &= x^{-2} \\
 f'(x) &= -2x^{-3} \\
 &= -\frac{2}{x^3}
 \end{aligned}$$

$$\begin{aligned}
 x > 0 \therefore x^3 > 0 \\
 \therefore f'(x) &= \frac{-2}{\text{positive}} \\
 &= \text{negative}
 \end{aligned}$$

7a) D(-1; 4)

$$\begin{aligned}
 b) h(x) &= -x^2 + 4 - 4 \\
 h(x) &= -x^2
 \end{aligned}$$

c) $x > 0$ or $x \leq 0$

4

d) $p = 1; q = 1$ (2)

e) At C and E, $x = 0$
 $\therefore y = \frac{-2}{1} + 1$

C: $y = -1^2 + 4$
 $= 3$

$\therefore CE = 4$ units (3)

8a) $x = -2$ or 3 (10) (2)

b) $-2 < x < 3$ (2)

c) -4 (1)

d) A of S; $x = 6$
 \therefore By symmetry, $OC = 1$ (2) (7)

9a) $f'(x) = 3ax^2 + 2bx - 5$
 $\therefore t = -5$ (2)

b) $f(2) = 0$ (from graph)
 $\therefore g(0) = -5$ (2)

c) $m = \frac{50-0}{0-(-5)}$
 $= \frac{10}{1}$ (2)

5

5

4 (14)

5

1d) $f''(x) = 0$ when
 $ac = \frac{-5 - \frac{1}{2}}{2}$

$x = -\frac{8}{3}$
 $\therefore f''(x) < 0$ when
 $x > -\frac{8}{3}$

e) $-5 < x < -\frac{8}{3}$ (2)

10) $\hat{R} = 90^\circ$ ($\angle n$ semi c) (11)

$q = 10 - p$
 $area = \frac{1}{2} p q$
 $= \frac{1}{2} p (10 - p)$
 $A = 5p - \frac{1}{2} p^2$
 $\frac{dA}{dp} = 5 - p$

At max, $5 - p = 0$
 $\therefore p = 5$
 $\therefore q = 5$

$PA^2 = 5^2 + 5^2$
 $PA = 5\sqrt{2}$ (8)

11c) $s(28)$
 $= -0,036(28)^2 + 2,02(28) + 1,78$ (2)
 $= 40,1$ mPa

b) $-0,036(2,02t + 1,78) = 24$
 $-0,036t^2 + 2,02t - 12,22 = 0$
 $t = 49,2$; $t = 6,9$ (4)
 \therefore 7th day.

c) $S'(t) = -9,072t + 2,02$
 $S'(21) = -9,072(21) + 2,02$
 $= 0,5$ (3)

19

12a) $S_1: 51; 49; 47, \dots$
 $S_n = \frac{a}{2} \{2(51) + (n-1)(-2)\}$
 $= \frac{a}{2} \{102 - 2n + 2\}$
 $= \frac{a}{2} \{104 - 2n\}$
 $= 52n - n^2$ (3)

b) $b: 25; 24; 23, \dots$
 $S_n = \frac{a}{2} \{2(25) + (n-1)(-1)\}$
 $= \frac{a}{2} \{50 - n + 1\}$
 $= \frac{a}{2} \{51 - n\}$
 $= \frac{a}{2} n - \frac{1}{2} n^2$

$52n - n^2 + \frac{a}{2} n - \frac{1}{2} n^2 = 1500$
 $104n - 2n^2 + 51n - n^2 = 2000$
 $0 = 3n^2 - 155n + 2000$
 $n \neq \frac{2000}{3}$ or $n = 25$ (5)

18

13) $(24-23)(24+23) + (22-21)(22+21)$
 $+ (20-19)(20+19) + \dots + (2-1)(2+1)$
 $= 47 + 43 + 39 + \dots + 3$
 $\therefore AS; a = 47; d = -4; n = 12$
 $S_{12} = 6 \{2(47) + 11(-4)\}$
 $= 300$ (5)

15

6

14) $9,3^{200} + m \cdot 3^{200} = 81 - m^2$
 $3^{200}(9+m) = (9-m)(9+m)$
 $3^{200} = \frac{(9-m)(9+m)}{9+m}$
 $3^{200} = 9 - m$ (2)

2

b) RHS must be a power of 3
 $\therefore m = 8$ (4)

14