



education

Department:
Education
REPUBLIC OF SOUTH AFRICA

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MATHEMATICS P2

NOVEMBER 2009(1)

MEMORANDUM

MARKS: 150

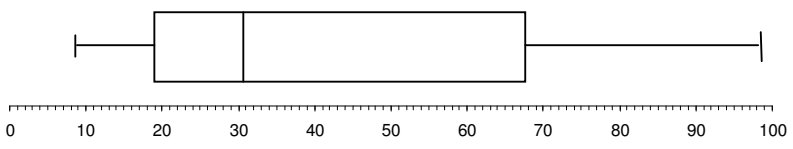
This memorandum consists of 25 pages.

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 1

1.1	$\text{Mean} = \frac{522,5}{12} = 43,5$ <p>ANSWER ONLY: Full marks</p>	✓ 522,5 ✓ answer (2) No penalty for Rounding: Accept 43,54 ; 44
1.2	<p>Ordered Data</p> <p>9,3 14,9 15 23,6 26,1 28 32,5 60,9 65,7 71,9 76,4 98,2</p> $\text{Median} = \frac{28 + 32,5}{2} = 30,3$ $\text{Lower quartile} = \frac{15 + 23,6}{2} = 19,3$ $\text{Upper quartile} = \frac{65,7 + 71,9}{2} = 68,8$ <p>The five number summary is (9,3 ; 19,3 ; 30,25 ; 68,8 ; 98,2) OR If they use the formula: Ordered Data</p> <p>9,3 14,9 15 23,6 26,1 28 32,5 60,9 65,7 71,9 76,4 98,2</p> $P_{50} = \frac{12+1}{2} = 6,5$ <p>Position of median: $\therefore Q_2 = \frac{28 + 32,5}{2} = 30,3$</p> $\text{Position of lower quartile: } P_{25} = \frac{13}{4}$ $\therefore Q_1 = 15 + (0,25(23,6 - 15)) = 17,15$ <p>Position of upper quartile: $P_{75} = 0,75(13) = 9,75$ $\therefore Q_3 = 65,7 + (0,75(71,9 - 65,7)) = 70,35$ Min = 9,3 Max = 98,2</p> <p>Accept any one of these five number summaries: (9,3 ; 19,3 ; 30,3 ; 68,8 ; 98,2) (9,3 ; 15 ; 30,3 ; 71,9 ; 98,2) (9,3 ; 17,2 ; 30,3 ; 70,4 ; 98,2)</p>	✓ 9,3 ✓ 19,3 ✓ 30,3 ✓ 68,8 ✓ 98,2 (5) If indicated on the box and whisker diagram in 1.3 – 5 marks

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

<p>1.3</p>	 <div style="border: 1px solid black; padding: 5px; margin: 10px auto; width: fit-content;"> <p>Note: If just a box and whisker without any reference to the numbers: 1/3</p> </div>	<p>✓ minimum and maximum values ✓ quartiles and median ✓ whiskers with median line</p> <p style="text-align: right;">(3)</p>																																										
<p>1.4</p>	<p>The data is skewed to the right (positively skewed). This suggests that there was a large difference between the median and the maximum rainfall (some months had exceptionally high rainfall in that year).</p> <p><i>Die data is skeef na regs (positief skeef) Dit dui daarop dat daar 'n groot verskil is tussen die mediaan en die maksimum reënval (sommige maande het ongewoon hoë reënval gehad gedurende die jaar.</i></p>	<p>✓ ✓ comment about rainfall. (2)</p> <p>Note: Skewed to right 1/2</p> <p>✓ ✓ verwysing na reënval (2)</p>																																										
<p>1.5</p>	<p>By using the calculator, $\sigma = 28,19$. (28,19058256)</p> <p>OR Pen and Paper method (not recommended) Mean = 43,54 (43,54166667)</p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th>x</th> <th>$x - \bar{x}$</th> <th>$(x - \bar{x})^2$</th> </tr> </thead> <tbody> <tr><td>60,9</td><td>17,36</td><td>301,3696</td></tr> <tr><td>14,9</td><td>-28,64</td><td>820,2496</td></tr> <tr><td>9,3</td><td>-34,24</td><td>1172,378</td></tr> <tr><td>28,0</td><td>-15,54</td><td>241,4916</td></tr> <tr><td>71,9</td><td>28,36</td><td>804,2896</td></tr> <tr><td>76,4</td><td>32,86</td><td>1079,78</td></tr> <tr><td>98,2</td><td>54,66</td><td>2987,716</td></tr> <tr><td>65,7</td><td>22,16</td><td>491,0656</td></tr> <tr><td>26,1</td><td>-17,44</td><td>304,1536</td></tr> <tr><td>32,5</td><td>-11,04</td><td>121,8816</td></tr> <tr><td>23,6</td><td>-19,94</td><td>397,6036</td></tr> <tr><td>15,0</td><td>-28,54</td><td>814,5316</td></tr> <tr> <td>Sum</td> <td></td> <td>9536,509</td> </tr> </tbody> </table> <p>$\sigma = \sqrt{\frac{9536,509}{12}} = 28,19$ (28,19059.....)</p>	x	$x - \bar{x}$	$(x - \bar{x})^2$	60,9	17,36	301,3696	14,9	-28,64	820,2496	9,3	-34,24	1172,378	28,0	-15,54	241,4916	71,9	28,36	804,2896	76,4	32,86	1079,78	98,2	54,66	2987,716	65,7	22,16	491,0656	26,1	-17,44	304,1536	32,5	-11,04	121,8816	23,6	-19,94	397,6036	15,0	-28,54	814,5316	Sum		9536,509	<p>✓✓✓ answer Accept: 28 ; 28,2 ; 28,1 (3)</p> <p>✓ headings correct ✓ sum of the squares of the mean deviations</p> <p>✓ answer (3)</p> <p style="text-align: right;">[15]</p>
x	$x - \bar{x}$	$(x - \bar{x})^2$																																										
60,9	17,36	301,3696																																										
14,9	-28,64	820,2496																																										
9,3	-34,24	1172,378																																										
28,0	-15,54	241,4916																																										
71,9	28,36	804,2896																																										
76,4	32,86	1079,78																																										
98,2	54,66	2987,716																																										
65,7	22,16	491,0656																																										
26,1	-17,44	304,1536																																										
32,5	-11,04	121,8816																																										
23,6	-19,94	397,6036																																										
15,0	-28,54	814,5316																																										
Sum		9536,509																																										

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 2

2.1	Linear or Exponential	✓ answer (1)
2.2	<div data-bbox="316 451 1088 955" style="border: 1px solid black; padding: 5px;"> <p style="text-align: center;">Scatter plot of times taken by winners of men's 100 m freestyle at Olympic Games</p> </div> <div data-bbox="308 997 1079 1564" style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p style="text-align: center;">Scatter Plot of time taken by the winner of 100m Freestyle at Olympic Games</p> </div> <p style="margin-top: 20px;">For this set of data we will accept the straight line.</p>	<p>✓ ✓ line of best fit (2)</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

2.3	<p>The scatter plot shows an overall decrease in the time taken by the winner since 1972.</p> <p><i>Die spreidiagram dui 'n algehele afname in tye aangeteken deur die wenners vanaf 1972.</i></p> <p>OR</p> <p>Times are faster. <i>Tye is vinniger.</i></p> <p>OR</p> <p>Negative correlation between year and time.</p> <p><i>Negatiewe korrelasie tussen jaar en tyd.</i></p>	<p>✓ decrease/afname (1)</p>
2.4	<p>The top athletes of the world have turned professional. This allows them to train at the best facilities and receive the best coaching available.</p> <p>Also, equipment manufacturers are in competition with each other. In this case, manufacturers are designing swimsuits that assist swimmers</p> <p>Swimmers train harder and put in more effort.</p> <p><i>Die top atlete van die wêreld het professionele atlete geword. Dit laat hulle toe om by die beste fasiliteite te oefen en die beste afrigting te ontvang.</i></p> <p><i>Vervaardigers van voorraad is in kompetisie met mekaar. Hul ontwerp dus swembroeke wat die swemmers help.</i></p> <p><i>Swemmers oefen harder en gebruik meer tyd om te oefen.</i></p>	<p>✓ any acceptable reason relating to the trend (1)</p> <p>✓ enige aanvaarbare rede wat verband hou met die neiging. (1)</p>
2.5	<p>In the context of the times around these two observations, one can consider the efforts of 1976 and 1988 to be outliers. This shows that these athletes were exceptionally good swimmers at the time.</p> <p><i>Binne die konteks van tye gedurende hierdie twee waarnemings, kan die poging van 1976 and 1988 gesien word as uitskieters. Dit dui daarop dat hierdie atlete uitstekende swemmers was daardie tyd.</i></p>	<p>✓✓ acceptable reason in context (2)</p> <p>✓✓ aanvaarbare rede binne die konteks (2)</p>
2.6	<p>Winning time of 2008 is expected to be about 47,6 seconds.</p> <p>Accept answer from candidate's graph.</p>	<p>✓ answer from graph (1)</p> <p>[8]</p>

QUESTION 3

3.1	50	<p>✓ answer (1)</p>
3.2	<p>Cut-off mark of 56% (37 students) or 58% (38 students)</p> <p>Accept interval: 55% - 60%</p>	<p>✓ answer read off from ogive (1)</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

3.3	<table border="1"> <thead> <tr> <th>Marks (out of 100)</th> <th>Frequency (<i>f</i>)</th> </tr> </thead> <tbody> <tr> <td>$0 \leq \text{marks} < 10$</td> <td>1</td> </tr> <tr> <td>$10 \leq \text{marks} < 20$</td> <td>3</td> </tr> <tr> <td>$20 \leq \text{marks} < 30$</td> <td>4</td> </tr> <tr> <td>$30 \leq \text{marks} < 40$</td> <td>11</td> </tr> <tr> <td>$40 \leq \text{marks} < 50$</td> <td>12</td> </tr> <tr> <td>$50 \leq \text{marks} < 60$</td> <td>9</td> </tr> <tr> <td>$60 \leq \text{marks} < 70$</td> <td>5</td> </tr> <tr> <td>$70 \leq \text{marks} < 80$</td> <td>4</td> </tr> <tr> <td>$80 \leq \text{marks} < 90$</td> <td>1</td> </tr> <tr> <td>$90 \leq \text{marks} < 100$</td> <td>0</td> </tr> </tbody> </table>	Marks (out of 100)	Frequency (<i>f</i>)	$0 \leq \text{marks} < 10$	1	$10 \leq \text{marks} < 20$	3	$20 \leq \text{marks} < 30$	4	$30 \leq \text{marks} < 40$	11	$40 \leq \text{marks} < 50$	12	$50 \leq \text{marks} < 60$	9	$60 \leq \text{marks} < 70$	5	$70 \leq \text{marks} < 80$	4	$80 \leq \text{marks} < 90$	1	$90 \leq \text{marks} < 100$	0	<p>✓ class intervals Accept $0 - 10 ; 10 - 20$ Or $0 < \text{marks} \leq 10$ Or Between 0 and 10 Or From 0 to 10</p> <p>If the intervals not in tens, the mark for intervals not given</p> <p>✓ method ✓ accuracy of five answers</p> <p style="text-align: right;">(3) [5]</p>
	Marks (out of 100)	Frequency (<i>f</i>)																						
	$0 \leq \text{marks} < 10$	1																						
	$10 \leq \text{marks} < 20$	3																						
	$20 \leq \text{marks} < 30$	4																						
	$30 \leq \text{marks} < 40$	11																						
	$40 \leq \text{marks} < 50$	12																						
	$50 \leq \text{marks} < 60$	9																						
	$60 \leq \text{marks} < 70$	5																						
	$70 \leq \text{marks} < 80$	4																						
	$80 \leq \text{marks} < 90$	1																						
$90 \leq \text{marks} < 100$	0																							

QUESTION 4

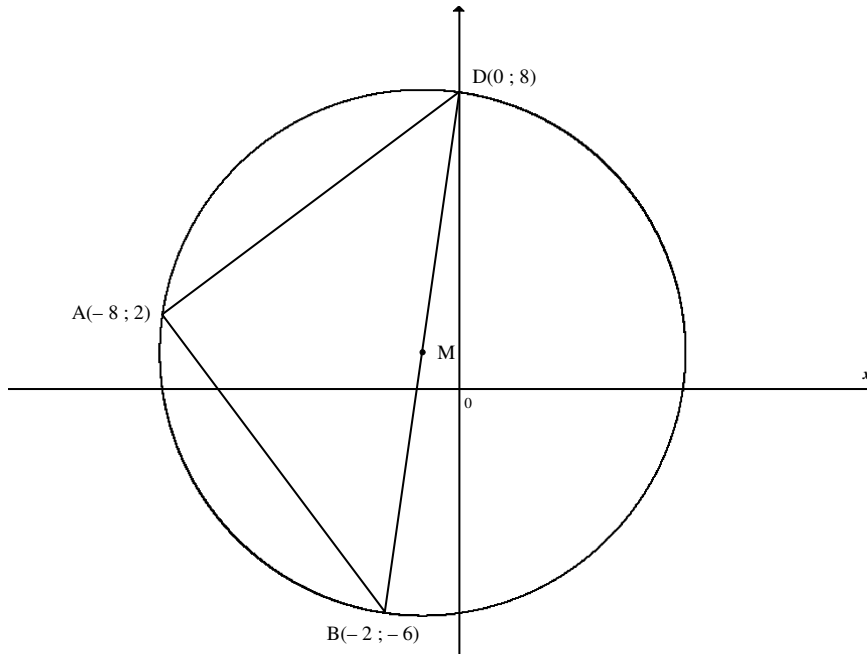
4.1	$\tan 45^\circ = m_{AB}$ $= 1$ OR $m_{AB} = \frac{3-0}{1-t} = \frac{3}{1-t}$	<p>✓ $\tan 45^\circ$ ✓ answer</p> <p style="text-align: right;">(2)</p> <p>Answer only: full marks</p>
4.2	$\frac{3-0}{1-t} = \tan 45^\circ = 1$ $1-t = 3$ $t = -2$ OR $y = mx + c$ $3 = (1)(1) + c$ $c = 2$ $y = x + 2$ $(t;0)$ in $y = mx + 2$ $0 = t + 2$ $t = -2$	<p>✓ equating</p> <p>✓ value</p> <p style="text-align: right;">(2)</p> <p>✓ $c=2$</p> <p>✓ value</p> <p style="text-align: right;">(2)</p> <p>Answer only: full marks</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

<p>4.3</p>	$\sqrt{(1-p)^2 + (3+4)^2} = \sqrt{50}$ $(1-p)^2 + (3+4)^2 = 50$ $1-2p + p^2 + 49 = 50$ $p^2 - 2p = 0$ $p(p-2) = 0$ $p \neq 0 \text{ or } p = 2$ <p>OR</p> $(1-p)^2 + (3+4)^2 = 50$ $(1-p)^2 = 50 - 49$ $(1-p)^2 = 1$ $1-p = 1 \quad \text{or} \quad 1-p = -1$ $p \neq 0 \quad \text{or} \quad p = 2$ <p>OR</p> <p>Let $p = 2$</p> $AC = \sqrt{(1-2)^2 + (3+4)^2}$ $= \sqrt{1+49}$ $= \sqrt{50}$ <p>which is true</p> <p>$\therefore p = 2$</p>	<ul style="list-style-type: none"> ✓ substitution into distance formula ✓ expansion ✓ factors ✓ answer <p>Note: If an answer was not chosen: 3/4</p> <p>(4)</p> <ul style="list-style-type: none"> ✓ substitution into distance formula ✓ expansion ✓ factors ✓ answer <p>(4)</p> <p>If gradient of BC assumed as -1 and p calculated correctly: 0/4</p> <p>Answer only: 1/4</p> <ul style="list-style-type: none"> ✓ substitution into distance formula ✓ $\sqrt{50}$ ✓ which is true(justification) ✓ answer <p>(4)</p> <p>If equating to $\sqrt{50}$ from the start, then 3/4</p>
<p>4.4</p>	<p>midpoint of BC = $\left(\frac{-2+2}{2}; \frac{0-4}{2}\right)$</p> <p>midpoint of BC = $(0; -2)$</p>	<ul style="list-style-type: none"> ✓ x-value ($x = \frac{t+p}{2}$) ✓ y-value <p>(2)</p>
<p>4.5</p>	<p>Gradient of line = $m_{AB} = 1$</p> <p>Equation of line is: $y + 4 = 1(x - 2)$</p> $y = x - 6$ <p>OR</p> $y = mx + c$ $y = x - p - 4$	<ul style="list-style-type: none"> ✓ gradients are equal ✓ substitution of $(p;-4)$ ✓ equation in any form <p>(3)</p> <p>[13]</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 5



5.1	Midpoint BD $\left(\frac{0-2}{2}; \frac{8-6}{2}\right)$ $= (-1; 1)$	✓ x-coordinate ✓ y-coordinate (2)
5.2	$y = 7(-8) + 58$ $= 2$ $\therefore A$ lies on the line.	✓ substitution (1) Substitute both at the same time with justification (1)
5.3	The line $y = 7x + 58$ is a tangent to the circle at A. $m_{line} = 7$ $m_{AM} = \frac{2-1}{-8-(-1)} = -\frac{1}{7}$ $m_{line} \times m_{AM} = 7 \times -\frac{1}{7} = -1$ $\therefore AM \perp$ to the line OR	✓ relationship $\checkmark\checkmark m_{AM} = \frac{2-1}{-8-(-1)} = -\frac{1}{7}$ $\checkmark m_{line} = 7$ \checkmark product (5)

NOTE:
 $m_{line} = 7$ and CA gradient of AM then no relationship: 4/5

NSC – Memorandum

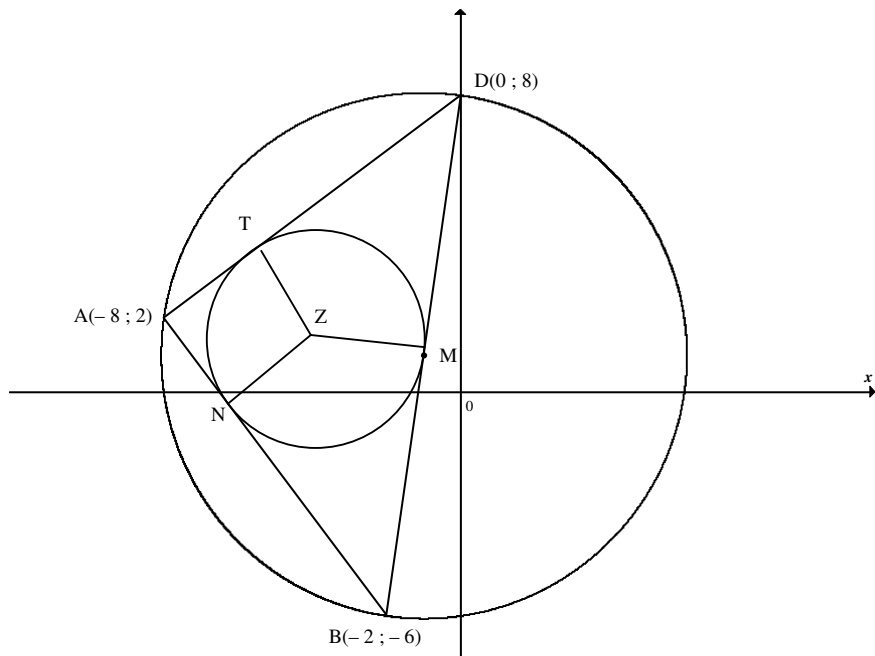
- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

5.3 contd	<p>OR</p> $m_{BD} = 7$ $m_{line} = 7$ <p>\therefore line // diameter</p> <p>OR</p> $(x+1)^2 + (y-1)^2 = 50$ $x^2 + 2x + 1 + y^2 - 2y + 1 = 50$ $x^2 + 2x + 1 + (7x + 58)^2 - 2(7x + 58) + 1 = 50$ $x^2 + 2x + 1 + 49x^2 + 812x + 3364 - 14x - 116 + 1 = 50$ $50x^2 + 800x + 3200 = 0$ $x^2 + 16x + 64 = 0$ $(x+8)^2 = 0$ $x = -8$ $y = 2$ $y = 7x + 58 \text{ is a tangent to the circle}$	$\checkmark\checkmark m_{BD} = 7$ $\checkmark m_{line} = 7$ $\checkmark\checkmark$ conclusion (5) Note: Only lines parallel 4/5 \checkmark circle equation \checkmark substitution of $y = 7x + 58$ \checkmark standard form \checkmark answer \checkmark tangent (5)
5.4	$AD = \sqrt{(8-2)^2 + (0+8)^2}$ $= \sqrt{36 + 64}$ $= 10$ $AB = \sqrt{(2+6)^2 + (-8+2)^2}$ $= \sqrt{64 + 36}$ $= 10$	\checkmark substitution \checkmark answer \checkmark substitution \checkmark answer (4) Note: Answers $\sqrt{10}$ then 3/4

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

<p>5.5</p>	$m_{AD} = \frac{8 - (2)}{0 - (-8)}$ $m_{AD} = \frac{3}{4}$ $m_{AB} = \frac{2 - (-6)}{-8 - (-2)}$ $= -\frac{4}{3}$ $m_{AB} \cdot m_{AD} = -\frac{4}{3} \times \frac{3}{4}$ $= -1$ $\hat{DAB} = 90^\circ$ <p>OR</p> $BD^2 = (8 + 6)^2 + (0 + 2)^2$ $= 200$ $= AD^2 + AB^2$ $\therefore \hat{DAB} = 90^\circ$ <p>OR</p> $a^2 = b^2 + d^2 - 2(b)(d) \cos A$ $200 = 100 + 100 - 2(10)(10) \cos A$ $0 = -200 \cos A$ $A = 90^\circ$ <p>OR</p> $(AD)^2 = 100$ $(AB)^2 = 100$ $BD^2 = (-2 - 0)^2 + (-6 - 8)^2$ $= 4 + 196$ $= 200$ $\therefore BD^2 = AD^2 + AB^2$ $\therefore \hat{DAB} = 90^\circ \quad (\text{Pyth})$ <p>OR</p> $\hat{A} = 90^\circ \quad (\text{angles in semi - circle})$	<p>✓ gradient of AD</p> <p>✓ gradient of AB</p> <p>✓ PRODUCT (3)</p> <p>✓ distance formula</p> <p>✓ Pythagoras ✓ conclusion (3)</p> <p>✓ cos rule ✓ substitution ✓ conclusion (3)</p> <p>✓ $BD^2 = 200$</p> <p>✓ $BD^2 = AD^2 + AB^2$ ✓ conclusion (3)</p> <p>✓ ✓ ✓ reason (3)</p>
<p>5.6</p>	$\theta = 45^\circ$	<p>✓ answer (1)</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.



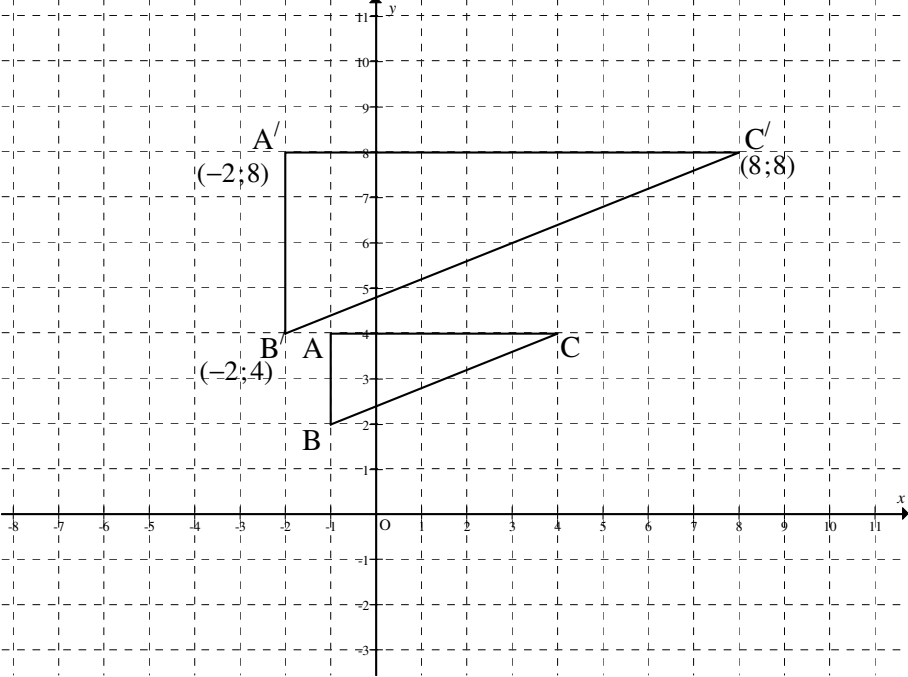
<p>5.7</p>	<p>Let the radius of circle TNM be r $NB = BM$ (properties of a kite) $AN = TZ = r$ (TZNA is a square) $NB = 10 - r$ $BD = 2MB$ $\sqrt{(8 - (-6))^2 + (0 - (-2))^2} = 2(10 - r)$ $\sqrt{200} = 2(10 - r)$ $10\sqrt{2} = 2(10 - r)$ $r = 10 - 5\sqrt{2}$ $= 2,93$</p> <p>OR</p> <p>$\hat{ZMB} = 90^\circ$ $MB = \frac{1}{2}\sqrt{200}$ $= 7,07$ $\frac{ZM}{MB} = \tan 22,5^\circ$ $ZM = 7,07 \tan 22,5^\circ$ $= 2,93$</p> <p>OR</p>	<p>✓ $NB = BM$ ✓ $AN = TZ = r$ ✓ $NB = 10 - r$ ✓ $BD = 2MB$ ✓ $BD = \sqrt{200}$</p> <p>✓ answer (6)</p> <p>✓ tan radius theorem</p> <p>✓ ✓ MB</p> <p>✓ ✓ $\tan 22,5^\circ$</p> <p>✓ answer (6)</p>
------------	---	---

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

5.7 contd	$MB^2 = (-1+2)^2 + (1+6)^2$ $= 1 + 49$ $= 50$ $MB = \sqrt{50}$ $\frac{ZM}{MB} = \tan 22,5^\circ$ $ZM = 7,07 \tan 22,5^\circ$ $= 2,93$ <p>OR</p> <p>By a well known formula</p> <p>Area $\Delta ABD = r \times (\text{semi—perimeter})$</p> $\frac{1}{2} \times 10 \times 10 = r \times \frac{1}{2} (20 + \sqrt{200})$ $50 = r(10 + 5\sqrt{2})$ $r = 2,93$ <p>OR</p> $MB = \sqrt{50} \quad (\text{radius of circle})$ $NB = \sqrt{50} \quad (\text{adjacent sides of kite})$ $AB = 10$ $AN = 10 - \sqrt{50}$ $= 2,93$ <p>But TANZ is a square</p> $\therefore AN = ZN$ $\therefore \text{radius} = 2,93$	<p>✓✓ MB</p> <p>✓✓ $\tan 22,5^\circ$</p> <p>✓✓ answer (6)</p> <p>✓✓ formula</p> <p>✓ $\sqrt{200}$</p> <p>✓✓ answer (6)</p> <p>✓ MB</p> <p>✓ NB</p> <p>✓✓ AN = 2,93</p> <p>✓ square</p> <p>✓ answer (6)</p>
--------------	--	--

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 6

6.1.1	$4 \times 5 = 20$ squared units	✓✓ answer $2^2 \times 5$ 1/2 If $2 \times 5 = 10$ 0/2 (2)
6.1.2	$(x; y) \rightarrow (2x; 2y)$ Note: If candidate state: coordinates times two 2/2	✓ $2x$ ✓ $2y$ (2) If $(kx; ky): 1/2$ If $2(x; y): 2/2$
6.1.3		✓ coordinates A' ✓ coordinates B' ✓ coordinates C' (3) If diagram not drawn but coordinates correctly given: 1/3 If coordinates correctly plotted but not joined: 2/3
6.1.4	Not rigid. The shape remains the same, whilst the size is changed /enlarged Note: Shape remains the same: 1/2 Only the shape remains the same: 2/2	✓✓ same shape and different size (2) not rigid only 2/2 just enlarged 0/2
6.2	Reflection about the line $y = x$: $(x; y) \rightarrow (y; x)$ Rotate clockwise about the origin: $(y; x) \rightarrow (x; -y)$ Translate 2 left and 3 down: $(x; -y) \rightarrow (x - 2; -y - 3)$ OR General rule: $(x; y) \rightarrow (x - 2; -y - 3)$	Mark per coordinate ✓✓ reflection ✓✓ rotation ✓✓ translation (6) Answer only: Full marks [15]

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	<p>OR</p> <p>The first 2 transformations in the given order is the same as the reflection in the x-axis i.e. $(x ; y) \rightarrow (x ; -y)$ Then the translation gives us $(x ; y) \rightarrow (x ; -y) \rightarrow (x - 2 ; -y - 3)$</p>	
	<p>NOTE: If just given: $(x ; y) \rightarrow (x - 2 ; y - 3)$: 2/6</p> <p>If using $(x ; y) \rightarrow (y ; x)$ ✓✓ $(x ; y) \rightarrow (y ; -x)$ ✓ $(x ; y) \rightarrow (x - 2 ; y - 3)$ ✓ throughout :4/6</p>	<p>If learner starts with $(x ; y)$ and continue to use $(x ; y)$ for the second and third transformation 4/6</p>

QUESTION 7

7.1	$T' (x \cos \theta - y \sin \theta ; y \cos \theta + x \sin \theta)$	✓ x coordinate ✓ y coordinate (2) Clock-wise formula: 0/2
7.2	$A' (p \cos 135^\circ - q \sin 135^\circ ; q \cos 135^\circ + p \sin 135^\circ)$ If clockwise rotation: $A' (p \cos 135^\circ + q \sin 135^\circ ; q \cos 135^\circ - p \sin 135^\circ)$	✓ x coordinate ✓ y coordinate (2) CA from 7.1
7.3	$x' = p \cos(135^\circ) - q \sin(135^\circ)$ $-1 - \sqrt{2} = -p \cos 45^\circ - q \sin 45^\circ$ $-1 - \sqrt{2} = -p \left(\frac{\sqrt{2}}{2} \right) - q \left(\frac{\sqrt{2}}{2} \right)$ $-1 - \sqrt{2} = -\frac{\sqrt{2}}{2} p - \frac{\sqrt{2}}{2} q \dots \dots \dots (1)$ and $y' = y \cos(135^\circ) + p \sin(135^\circ)$ $1 - \sqrt{2} = -q \cos 45^\circ + p \sin 45^\circ$ $1 - \sqrt{2} = q \left(-\frac{\sqrt{2}}{2} \right) + p \left(\frac{\sqrt{2}}{2} \right)$ $1 - \sqrt{2} = -\frac{\sqrt{2}}{2} q + \frac{\sqrt{2}}{2} p \dots \dots \dots (2)$ (1) + (2): $-2\sqrt{2} = -\sqrt{2}q$ $q = 2$	✓ equating ✓ substitution ✓ equating ✓ substitution $\frac{\sqrt{2}}{2}$ ✓ solving simultaneously

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

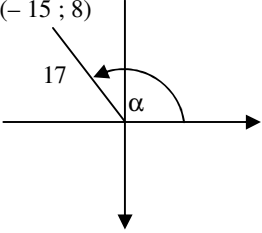
	<p>Substitute $q = 2$ into(1)</p> $-1 - \sqrt{2} = -\frac{\sqrt{2}}{2}p - \frac{\sqrt{2}}{2} \quad (2)$ $-1 = -\frac{\sqrt{2}}{2}p$ $p = \sqrt{2}$ $\therefore A = (\sqrt{2}; 2)$ <p>OR</p> $x' = p \cos(135^\circ) - q \sin(135^\circ)$ $-1 - \sqrt{2} = -p \cos 45^\circ - q \sin 45^\circ$ $-1 - \sqrt{2} = -p \left(\frac{\sqrt{2}}{2} \right) - q \left(\frac{\sqrt{2}}{2} \right)$ $-1 - \sqrt{2} = -\frac{\sqrt{2}}{2}p - \frac{\sqrt{2}}{2}q \dots\dots\dots(1)$ <p>and</p> $y' = y \cos(135^\circ) + p \sin(135^\circ)$ $1 - \sqrt{2} = -q \cos 45^\circ + p \sin 45^\circ$ $1 - \sqrt{2} = q \left(-\frac{\sqrt{2}}{2} \right) + p \left(\frac{\sqrt{2}}{2} \right)$ $-0,41 = -0,71q + 0,71p \dots\dots\dots(2)$ <p>(1) + (2):</p> $-2\sqrt{2} = -\sqrt{2}q$ $q = 2$ <p>Substitute $q = 2$ into(1)</p> $-2,41 = -0,71p - 0,71q \quad (2)$ $1,42p = 2$ $p = 1,41$ $\therefore A = (\sqrt{2}; 2)$	<p>✓ answer for q</p> <p>✓ answer for p</p> <p>(7)</p> <p>✓ equating</p> <p>✓ substitution</p> <p>✓ equating</p> <p>✓ substitution $\frac{\sqrt{2}}{2}$</p> <p>✓ solving simultaneously</p> <p>✓ answer for q</p> <p>✓ answer for p</p> <p>(7)</p>
OR		

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	$-\frac{\sqrt{2}}{2}(p+q) = -1 - \sqrt{2}$ $p+q = -\frac{2}{\sqrt{2}}(-1 - \sqrt{2})$ $p+q = \sqrt{2} + 2$ <p>and</p> $\frac{1}{\sqrt{2}}(p-q) = 1 - \sqrt{2}$ $p-q = \sqrt{2} - 2$ $p+q = \sqrt{2} + 2$ $2p = 2\sqrt{2}$ $p = \sqrt{2}$ $q = 2$ <p>OR</p> <p>$A(p; q)$ is obtained from A' by a rotation through 135° in a clockwise direction</p> $p = (-1 - \sqrt{2})\cos(-135^\circ) - (1 - \sqrt{2})\sin(-135^\circ)$ $= (-1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right) - (1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right)$ $= \frac{2}{\sqrt{2}}$ $= \sqrt{2}$ $q = (1 - \sqrt{2})\cos(-135^\circ) + (-1 - \sqrt{2})\sin(-135^\circ)$ $= (1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right) + (-1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right)$ $= \frac{2\sqrt{2}}{\sqrt{2}}$ $= 2$ $\therefore A = (\sqrt{2}; 2)$	<p>✓</p> $-\frac{\sqrt{2}}{2}(p+q) = -1 - \sqrt{2}$ <p>✓ substitution</p> <p>✓ $\frac{1}{\sqrt{2}}(p-q) = 1 - \sqrt{2}$</p> <p>✓ substitution $\frac{\sqrt{2}}{2}$</p> <p>✓ solving simultaneously</p> <p>✓ answer for q</p> <p>✓ answer for p</p> <p>(7)</p> <p>✓ substituting $(-1 - \sqrt{2})$</p> <p>✓ substitution $\frac{1}{\sqrt{2}}$</p> <p>✓ equating</p> <p>✓ substitution $\frac{1}{\sqrt{2}}$</p> <p>✓ substituting $(-1 - \sqrt{2})$</p> <p>✓ answer for q</p> <p>✓ answer for p</p> <p>(7)</p>
--	--	--

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 8

<p>8.1</p>	<p> $\sin \alpha = \frac{8}{17}$ $\sin \alpha > 0 \therefore$ in second quadrant $y_\alpha = 8 \quad r_\alpha = 17$ $x_\alpha = -15$ (Pythagoras) $\tan \alpha = -\frac{8}{15}$ </p> 	<p> $x = -\sqrt{15}$✓ ✓ answer (3) For drawing the radius vector in the correct quadrant 1/3 Without a sketch but correct values: 3/3 </p>
<p>8.2</p>	<p> $\sin(90^\circ + \alpha) = \cos \alpha$ $= -\frac{15}{17}$ </p>	<p> ✓ reduction ✓ answer (2) Answer only: full marks Cannot accept decimal values </p>
<p>8.3</p>	<p> $\cos 2\alpha = 1 - 2 \sin^2 \alpha$ $= 1 - 2\left(\frac{8}{17}\right)^2$ $= \frac{161}{289}$ OR $\cos 2\alpha = 2 \cos^2 \alpha - 1$ $= 2\left(\frac{-15}{17}\right)^2 - 1$ $= \frac{161}{289}$ OR $\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$ $= \left(\frac{-15}{17}\right)^2 - \left(\frac{8}{17}\right)^2$ $= \frac{161}{289}$ </p>	<p> ✓ expansion ✓ substitution ✓ any further calculation or answer (3) ✓ expansion ✓ substitution ✓ any further calculation or answer (3) ✓ expansion ✓ substitution ✓ any further calculation or answer (3) [8] </p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 9

NOTE: Only penalise once in the question for leaving out the x
 Penalise once in this question for treating as an equation

9.1	$\sin(90^\circ - x) \cdot \cos(180^\circ - x) + \tan x \cdot \cos(-x) \cdot \sin(180^\circ + x)$ $= \cos x(-\cos x) + \tan x(\cos x)(-\sin x)$ $= -\cos^2 x - \frac{\sin x}{\cos x} \cos x \sin x$ $= -\cos^2 x - \sin^2 x$ $= -(\cos^2 x + \sin^2 x)$ $= -1$	<ul style="list-style-type: none"> ✓ $\sin(90^\circ - x) = \cos x$ ✓ $\cos(180^\circ - x) = -\cos x$ ✓ $\cos(-x) = \cos x$ ✓ $\sin(180^\circ + x) = -\sin x$ ✓ $\tan x = \frac{\sin x}{\cos x}$ ✓ simplification ✓ answer <p style="text-align: right;">(7)</p>
9.2	$\frac{\sin 190^\circ \cos 225^\circ \tan 390^\circ}{\cos 100^\circ \sin 135^\circ}$ $= \frac{-\sin 10^\circ(-\cos 45^\circ) \tan 30^\circ}{-\sin 10^\circ \sin 45^\circ}$ $= \frac{-\frac{1}{\sqrt{2}} \cdot \frac{1}{\sqrt{3}}}{\frac{1}{\sqrt{2}}}$ <p style="text-align: center;">or</p> $= -\tan 30^\circ$ $= -\frac{1}{\sqrt{3}}$	<ul style="list-style-type: none"> ✓ $\sin 190^\circ = -\sin 10^\circ$ ✓ $\cos 225^\circ = -\cos 45^\circ$ ✓ $\tan 390^\circ = \tan 30^\circ$ ✓ $\cos 100^\circ = -\sin 10^\circ$ ✓ $\sin 135^\circ = \sin 45^\circ$ or $\cos 45^\circ$ <p>✓✓ substitution</p> <p style="text-align: right;">(7)</p>
9.3	$\sin x + 2\cos^2 x = 1$ $\sin x + 2(1 - \sin^2 x) = 1$ $-2\sin^2 x + \sin x + 1 = 0$ $2\sin^2 x - \sin x - 1 = 0$ $(2\sin x + 1)(\sin x - 1) = 0$ $\sin x = 1$ $x = 90^\circ + k \cdot 360^\circ; k \in Z$ <p>Or</p>	<ul style="list-style-type: none"> ✓ substitution of identity ✓ standard form ✓ factorisation ✓ $\sin x = 1; \sin x = -\frac{1}{2}$ ✓ $x = 90^\circ + k \cdot 360^\circ; k \in Z$ ✓✓ answers (any two answers) <p style="text-align: right;">(7)</p> <p>If $k \in Z$ not included: 6/7</p> <p>Also $\pm k \cdot 360^\circ; k \in N_0$ or Z</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

$\sin x = -\frac{1}{2}$ $x = 210^\circ + k.360^\circ; k \in Z \quad \text{OR} \quad x = 210^\circ + k.360^\circ$ $\text{or } x = 330^\circ + k.360^\circ; k \in Z \quad \text{or } x = -30^\circ + k.360^\circ$ <p>OR</p> $x = -150^\circ + k.360^\circ; k \in Z \quad \text{OR} \quad x = -150^\circ + k.360^\circ; k \in Z$ $\text{or } x = 330^\circ + k.360^\circ \quad \text{or } x = -30^\circ + k.360^\circ$ <p>OR</p> $\sin x + 2 \cos^2 x = 1$ $\sin x = 1 - 2 \cos^2 x$ $\sin x = -\cos 2x$ $\sin x = -[\sin(90^\circ - 2x)]$ $x = 180^\circ + (90^\circ - 2x) + k360^\circ$ $3x = 270^\circ + k360^\circ \quad \text{or} \quad x = 360^\circ - (90^\circ - 2x) + k360^\circ$ $x = 90^\circ + k120^\circ \quad x = -270^\circ - k360^\circ$ $k \in Z$ <p>OR</p> $\sin x + 2 \cos^2 x = 1$ $\sin x = 1 - 2 \cos^2 x$ $\sin x = -\cos 2x$ $-\cos(90^\circ - x) = \cos 2x$ $2x = 180^\circ - (90^\circ - x) + k360^\circ \quad 2x = 180^\circ + (90^\circ - x) + k360^\circ$ $x = 90^\circ + k360^\circ \quad \text{or} \quad 3x = 270^\circ + k360^\circ$ $x = 90^\circ + k360^\circ \quad x = 30^\circ + k120^\circ$ $k \in Z$	<ul style="list-style-type: none"> ✓ manipulation ✓ substitution of identity ✓ co ratios ✓ $x = 180^\circ + (90^\circ - 2x) + k360^\circ$ ✓ $x = 90^\circ + k120^\circ$ ✓ $x = 360^\circ - (90^\circ - 2x) + k360^\circ$ ✓ $x = -270^\circ - k360^\circ$ <p style="text-align: right;">(7)</p> <p>If $k \in Z$ not included: 6/7</p> <ul style="list-style-type: none"> ✓ manipulation ✓ substitution of identity ✓ co ratios ✓ $2x = 180^\circ - (90^\circ - x) + k360^\circ$ ✓ $x = 90^\circ + k360^\circ$ ✓ $2x = 180^\circ + (90^\circ - x) + k360^\circ$ ✓ $x = 30^\circ + k120^\circ$ <p style="text-align: right;">(7)</p> <p>If $k \in Z$ not included: 6/7</p> <p style="text-align: right;">[20]</p>
---	--

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 10

<p>10.1</p>	$\frac{\sin(A + B)}{\cos(A + B)} = \frac{\sin A \cdot \cos B + \cos A \cdot \sin B}{\cos A \cdot \cos B - \sin A \cdot \sin B}$ $= \frac{\sin A \cdot \cos B + \cos A \cdot \sin B}{\cos A \cdot \cos B - \sin A \cdot \sin B} \times \frac{1}{\frac{\cos A \cdot \cos B}{1}}$ $= \frac{\sin A \cdot \cos B}{\cos A \cdot \cos B} + \frac{\cos A \cdot \sin B}{\cos A \cdot \cos B}$ $= \frac{\sin A}{\cos A} + \frac{\sin B}{\cos B}$ $= \frac{\tan A + \tan B}{1 - \tan A \cdot \tan B}$ <p>OR</p> $RHS = \frac{\tan A + \tan B}{1 - \tan A \cdot \tan B}$ $= \frac{\frac{\sin A}{\cos A} + \frac{\sin B}{\cos B}}{1 - \frac{\sin A \cdot \sin B}{\cos A \cdot \cos B}} \times \frac{\cos A \cdot \cos B}{\cos A \cdot \cos B}$ $= \frac{\sin A \cos B + \sin B \cos A}{\cos A \cos B - \sin A \sin B}$ $= \frac{\sin(A + B)}{\cos(A + B)}$ $= \tan(A + B)$ <p>= LHS</p>	<p>✓ expansions</p> <p>✓ divisions</p> <p>✓ tanA and tanB (3)</p> <p>✓ $\frac{\sin A}{\cos A}$</p> <p>✓ multiplication</p> <p>✓ expansions (3)</p>
<p>10.2</p>	$\tan C = \tan(180^\circ - (A + B))$ $\tan C = -\tan(A + B)$ $\tan C = -\left(\frac{\tan A + \tan B}{1 - \tan A \cdot \tan B}\right)$ $\tan C(1 - \tan A \cdot \tan B) = -(\tan A + \tan B)$ $\tan C - \tan A \cdot \tan B \cdot \tan C = -\tan A - \tan B$ $\tan A + \tan B + \tan C = \tan A \cdot \tan B \cdot \tan C$ <p>OR</p>	<p>✓ C</p> <p>✓ $-\tan(A + B)$</p> <p>✓ substitution into formula</p> <p>✓ multiplication with LCD</p> <p>(4)</p> <p>If no conclusion: 3/4</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	$\hat{C} = 180^\circ - (\hat{A} + \hat{B}) \quad (\text{angles in a triangle})$ $\tan C = \tan(180^\circ - (A + B))$ $\tan C = \tan((180^\circ - A) + (-B))$ $\tan C = \frac{\tan(180^\circ - A) + \tan(-B)}{1 - \tan(180^\circ - A) \cdot \tan(-B)}$ $\tan C(1 - \tan(180^\circ - A) \cdot \tan(-B)) = \tan(180^\circ - A) + \tan(-B)$ $\tan C - \tan C \tan A \tan B = -\tan A - \tan B$ $\tan A + \tan B + \tan C = \tan A \cdot \tan B \cdot \tan C$	<p>✓ C</p> <p>✓ rearrange angle</p> <p>✓ substitution into formula</p> <p>✓ expansion</p> <p style="text-align: right;">(4)</p>
--	--	---

QUESTION 11

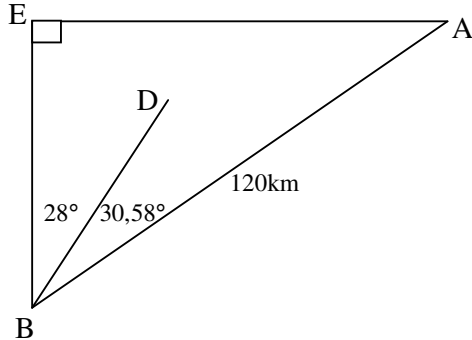
NOTE: Penalty of one for early rounding off once in this question

11.1.1	$\hat{BDA} = 208^\circ - 67^\circ$ $= 141^\circ$ $\frac{\sin \hat{DBA}}{97} = \frac{\sin 141^\circ}{120}$ $\sin \hat{DBA} = 0,5087006494\dots$ $\hat{DBA} = 30,58^\circ$ <p>∴ Bearing of Ship A from Ship B</p> $= 180^\circ - (360^\circ - 208^\circ) + 30,58^\circ$ $= 58,58^\circ$ <p>OR</p> $\hat{BDA} = 208^\circ - 67^\circ$ $= 141^\circ$ $\frac{\sin \hat{DBA}}{97} = \frac{\sin 141^\circ}{120}$ $\sin \hat{DBA} = 0,5087006494\dots$ $\hat{DBA} = 30,58^\circ$ <p>then $360^\circ - 208^\circ = \hat{NDB}$ (reflex angles)</p> $\therefore \hat{NDB} = 152^\circ$ <p>but $\hat{MBD} + \hat{NDB} = 180^\circ$ (co - interior angles/ angles around a point)</p> $\therefore \hat{MBD} = 28^\circ$ <p>then $\hat{MBA} = \hat{MBD} + \hat{DBA}$</p> $= 30,58^\circ + 28^\circ$ $= 58,58^\circ$	<p>✓ $\hat{BDC} = 141^\circ$</p> <p>✓ sine rule</p> <p>✓ substitution</p> <p>✓ $\hat{B} = 30,58^\circ$</p> <p>✓ method or</p> <p>$\hat{MBD} = 28^\circ$</p> <p>✓ answer</p> <p style="text-align: right;">(6)</p> <p>✓ $\hat{BDC} = 141^\circ$</p> <p>✓ sine rule</p> <p>✓ substitution</p> <p>✓ $\hat{NDB} = 152^\circ$</p> <p>✓ $\hat{MBD} = 28^\circ$</p> <p>✓ answer</p> <p style="text-align: right;">(6)</p>
--------	---	--

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

11.1.2

$\hat{B} = 30,58^\circ$

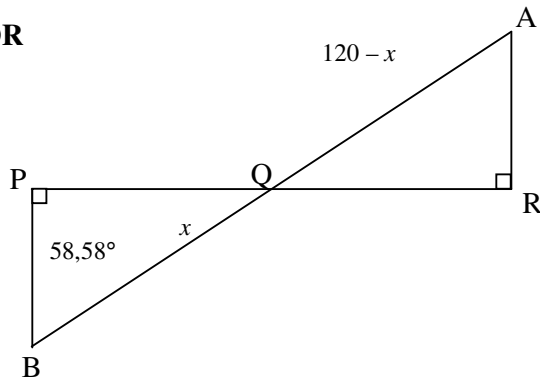


$$\frac{EA}{120} = \sin(28^\circ + 30,58^\circ)$$

$$EA = 120 \sin(28^\circ + 30,58^\circ)$$

$$EA = 102,4 \text{ km}$$

OR



Let $BQ = x$, then $AQ = 120 - x$

$$\sin 58,58^\circ = \frac{PQ}{x} \qquad \sin 58,58^\circ = \frac{QR}{120 - x}$$

$$PQ = x \cdot \sin 58,58^\circ \qquad QR = (120 - x) \sin 58,58^\circ$$

$$PQ + QR = x \cdot \sin 58,58^\circ + (120 - x) \sin 58,58^\circ$$

$$= 120 \sin 58,58^\circ$$

$$= 102,4$$

OR

$BP = AR$ (assume ships move at same speed)

✓ definition
✓ substitution

✓ answer
(3)

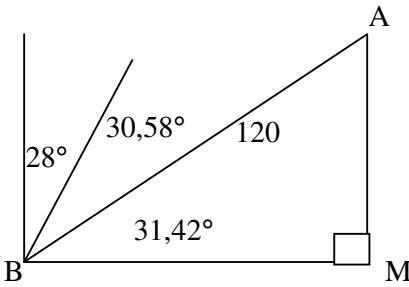
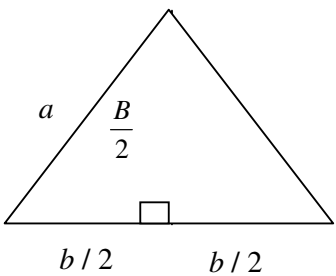
✓
trigonometric ratios

✓ sum

✓ answer
(3)

✓
trigonometric

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	<p>$\Delta PBQ \equiv \Delta RAQ$ (angle, angle, side)</p> <p>$\therefore BQ = QA = 60 \text{ km}$</p> <p>$\sin 58,58^\circ = \frac{PQ}{60}$</p> <p>$\therefore PQ = 60 \sin 58,58^\circ$</p> <p>$= 51,20 \text{ km}$</p> <p>$PR = 2PQ$</p> <p>$= 102,4 \text{ km}$</p> <p>OR</p> <p>$\frac{BM}{120} = \cos 31,42$</p> <p>$BM = 120 \times \cos 31,42^\circ$</p> <p>$= 102,4$</p> 	<p>ratios</p> <p>✓ 51,20 km</p> <p>✓ answer (3)</p> <p>✓ trigonometric ratios</p> <p>✓ substitution</p> <p>✓ answer (3)</p>
<p>11.2</p>	<p>$AB = BC = a = c$</p> <p>$b^2 = a^2 + c^2 - 2ac \times \cos B$</p> <p>$b^2 = a^2 + a^2 - 2a \times a \times \cos B$</p> <p>$b^2 = 2a^2 - 2a^2 \cos B$</p> <p>$b^2 = 2a^2(1 - \cos B)$</p> <p>$\frac{b^2}{2a^2} = 1 - \cos B$</p> <p>$\cos B = 1 - \frac{b^2}{2a^2}$</p> <p>OR</p> <p>$\sin \frac{B}{2} = \frac{b}{2a}$</p> <p>$\cos B = 1 - 2 \sin^2 \frac{B}{2}$</p> <p>$= 1 - 2 \left(\frac{b}{2a} \right)^2$</p> <p>$= 1 - \frac{b^2}{2a^2}$</p> 	<p>✓ equal sides</p> <p>✓ cos rule</p> <p>✓ substitution</p> <p>✓ simplification (4)</p> <p>✓ $\sin \frac{B}{2}$</p> <p>✓ $\sin \frac{B}{2} = \frac{b}{2a}$</p> <p>✓ formula</p> <p>✓ substitution (4)</p> <p>[13]</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

<p>OR</p> $\cos B = \frac{a^2 + c^2 - b^2}{2ac}$ <p>but $a = c$</p> $\cos B = \frac{a^2 + a^2 - b^2}{2a.a}$ $= \frac{2a^2 - b^2}{2a^2}$ $= 1 - \frac{b^2}{2a^2}$	<p>✓ cos rule ✓ equal sides ✓ substitution ✓ simplification (4)</p>
--	---

QUESTION 12

<p>12.1</p>		<p>✓ (120°; 0) or (-60°; 0) ✓ (30°; 2) or (210°; -2) (2)</p>
-------------	--	---

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

QUESTION 12

12.2	$\cos(x - 30^\circ) = \frac{1}{2}$ $2 \cos(x - 30^\circ) = 1$ <p>See points A and B on the graph</p> <p>Note: If drawn the line $y = \frac{1}{2}$ and put A and B on the graph: 0/2</p> <p>If A and B on the x-axis: 1/2</p> <p>If $A = -30^\circ$ and $B = 90^\circ$: 1/2</p>	<p>✓ manipulation</p> <p>✓ answer (2)</p> <p>A and B in the correct place on the graph: full marks</p>
12.3	$\cos(x - 30^\circ) = 0,5$ $x - 30^\circ = 60^\circ \quad \text{OR} \quad x - 30^\circ = -60^\circ$ $x = 90^\circ \quad \quad \quad x = -30^\circ$	<p>✓ 60° (ref angle)</p> <p>✓ 90°</p> <p>✓ -30° (3)</p> <p>Answer only: 3/3</p>
12.4	$g'(x) = 0$ is at maximum and minimum values of graph $x = 30^\circ; 210^\circ$	<p>✓✓ one for each x-value (2)</p>
12.5	$x \in [-90^\circ; -60^\circ) \cup (120^\circ; 270^\circ]$ <p>OR $-90^\circ \leq x < -60^\circ$ or $120^\circ < x \leq 270^\circ$</p> <p>OR If $x < -60^\circ$ or $x > 120^\circ$ 2/3</p>	<p>✓ notation (3)</p> <p>✓✓ critical values</p> <p>[12]</p>